

Package ‘asteRisk’

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Type Package

Title Computation of Satellite Position

Version 1.4.3

Description Provides basic functionalities to calculate the position of satellites given a known state vector. The package includes implementations of the SGP4 and SDP4 simplified perturbation models to propagate orbital state vectors, as well as utilities to read TLE files and convert coordinates between different frames of reference. Several of the functionalities of the package (including the high-precision numerical orbit propagator) require the coefficients and data included in the 'asteRiskData' package, available in a 'drat' repository. To install this data package, run `'install.packages("`asteRiskData", repos=`https://rafael-ayala.github.io/drat/")'`.
Felix R. Hoots, Ronald L. Roehrich and T.S. Kelso (1988) <<https://celestrak.org/NORAD/documentation/spacetrk.pdf>>.
David Vallado, Paul Crawford, Richard Hujsak and T.S. Kelso (2012) <[doi:10.2514/6.2006-6753](https://doi.org/10.2514/6.2006-6753)>.
Felix R. Hoots, Paul W. Schumacher Jr. and Robert A. Glover (2014) <[doi:10.2514/1.9161](https://doi.org/10.2514/1.9161)>.

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BugReports <https://github.com/Rafael-Ayala/asteRisk/issues>

Additional_repositories <https://rafael-ayala.github.io/drat/>

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R topics documented:

calculateRazel	3
dateTimeToMJD	4
deg2rad	5
ECItokOE	6
GCRFtoITRF	7
GCRFtoLATLON	9
getLatestSpaceData	10
hpop	12
ITRFtoGCRF	15
ITRFtoLATLON	16
JPLephemerides	18
KOEtoECI	19
LATLONtoGCRF	21
LATLONtoITRF	22
parseTLElines	23
rad2deg	25
readGLONASSNavigationRINEX	26
readGPSNavigationRINEX	28
readOEM	33
readTLE	35
revDay2radMin	37
sdp4	38
sgdp4	40
sgp4	42
TEMEtoGCRF	44
TEMEtoITRF	45
TEMEtoLATLON	47

Index **49**

calculateRazel	<i>Calculates azimuth, elevation and range of a given object</i>
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Description

The horizontal coordinate system, also called azimuth-elevation system, uses the local horizon of an observer as its fundamental plane. In it, a given point is defined by 2 main angles: azimuth and elevation. Azimuth defines the angle of the point around the horizon in the X-Y plane, measured from the true North and usually increasing towards the East. Elevation is the angle between the object and the X-Y plane. Finally, the range defines the distance between the observer and the point.

This function calculates the azimuth, elevation and range given the coordinates of an observed satellite and of an observer. Both sets of coordinates must be provided as Cartesian geocentric coordinates in ITRF.

Usage

```
calculateRazel(geocentricObserver, geocentricSatellite, degreesOutput=TRUE)
```

Arguments

geocentricObserver	Vector with the X, Y and Z components of the position of the observer in ITRF frame.
geocentricSatellite	Vector with the X, Y and Z components of the position of the satellite in ITRF frame.
degreesOutput	Logical indicating if the output should be in sexagesimal degrees. If degreesOutput=FALSE, the output will be in radians.

Value

A vector with three elements, corresponding to the azimuth and elevation in degrees (or radians if specified) and the range in the same unit as the provided Cartesian coordinates.

References

https://gssc.esa.int/navipedia/index.php/Transformations_between_ECEF_and_ENU_coordinates

Examples

```
# The following were the coordinates of Italsat-2 in ITRF the 27th of June, 2006
# at 00:58:29.34 UTC, in meters.

italsat_ITRF <- c(-37325542.8, 19152438.3, 138384.5)

# Let us calculate its azimuth, elevation and range for an observer from Tokyo.
# The latitude and longitude of the city are 35.6762 degrees North, 139.6503
```

```
# degrees East. Let's assume an observer placed at sea level (0 m)
# We first convert these coordinates to ITRF:

observer_ITRF <- LATLONtoITRF(c(35.6762, 139.6503, 0), degreesInput=TRUE)

# We can now calculate the azimuth and elevation:

razel <- calculateRazel(observer_ITRF, italsat_ITRF, degreesOutput=TRUE)
razel[1] # Azimuth
razel[2] # Elevation
```

dateTimeToMJD

Calculate Modified Julian Date for a given date and time

Description

The Julian Date (JD) of a given date and time is the number of days since noon of Monday 1st of January 4713 BC, including a fractional part. Modified Julian Date (MJD) are instead the number of days since 00:00 of November 17th, 1858. The difference JD and MJD for a given instant is always 2400000.5, which is the JD of the reference time for MJD.

This function calculates the MJD of a date and time, provided as a date-time character string in UTC time. The output refers by default to the MJD in UTC, but different time systems can be chosen: UTC (Coordinated Universal Time), UT1 (Universal Time), TT (Terrestrial Time) and TDB (Barycentric Dynamical Time).

Usage

```
dateTimeToMJD(dateTime, timeSystem="UTC")
```

Arguments

dateTime	Date-time string with the date and time in UTC corresponding to the provided geodetic coordinates.
timeSystem	Time system into which the MJD should be calculated. Should be one from "UTC" (Coordinated Universal Time; default), "UT1" (Universal Time), "TT" (Terrestrial Time) and "TDB" (Barycentric Dynamical Time).

Value

The MJD for the specified date and time in the chosen time system.

References

https://gssc.esa.int/navipedia/index.php/Julian_Date https://gssc.esa.int/navipedia/index.php/Transformations_between_Tim

Examples

```
if(requireNamespace("asteRiskData", quietly = TRUE)) {  
  # Let's calculate the MJD of the 12th of June, 2000 at 10:00:00 UTC time, in UTC  
  
  MJD.UTC <- dateTimeToMJD("2000-06-12 10:00:00", timeSystem = "UTC")  
  
  # Let's now calculate the MJD for the same instant in TDB:  
  
  MJD.TDB <- dateTimeToMJD("2000-06-12 10:00:00", timeSystem = "TDB")  
  
  # We can now calculate the difference in seconds, which matches the difference  
  # between UTC and TDB for that day:  
  
  (MJD.UTC - MJD.TDB) * 86400  
}
```

deg2rad

Converts an angle in degrees to radians

Description

This function converts an angle in degrees to radians.

Usage

```
deg2rad(degrees)
```

Arguments

degrees Value of the angle in degrees.

Value

The corresponding value of the angle in radians.

Examples

```
deg2rad(180)
```

ECItoKOE

*Calculate ECI coordinates from Keplerian orbital elements***Description**

Keplerian orbital elements are a set of six parameters used to describe the orbits of celestial objects, including satellites. While satellites do not follow a perfectly Keplerian orbit, their state at any point can be defined by the orbital parameters that they would have if they were located at the same position with the same velocity following a perfectly Keplerian orbit (i.e., if perturbations were absent). These are called osculating orbital elements.

Keplerian orbital elements can be unequivocally determined from a satellite if its position and velocity are known. This function calculates orbital elements from the position and velocity of a satellite in an ECI (Earth-centered inertial) frame of reference. The elements (such as the equatorial plane) with respect to which the resulting orbital elements will be defined are the same as those used for the ECI frame of reference. The function calculates the six standard orbital elements, plus some alternative elements useful for the characterization of special orbits, such as circular ones or orbits with no inclination.

Usage

```
ECItoKOE(position_ECI, velocity_ECI)
```

Arguments

position_ECI	Vector with the X, Y and Z components of the position of an object in an ECI frame, in m.
velocity_ECI	Vector with the X, Y and Z components of the velocity of an object in an ECI frame, in m/s.

Value

A list with the following standard and alternative orbital elements:

semiMajorAxis	Semi-major axis of orbital ellipse in meters.
eccentricity	Numerical eccentricity of the orbit. Eccentricity measures how much the orbit deviates from being circular.
inclination	Inclination of the orbital plane in radians. Inclination is the angle between the orbital plane and the equator.
meanAnomaly	Mean anomaly of the orbit in radians. Mean anomaly indicates where the satellite is along its orbital path, and is defined as the angle between the direction of the perigee and the hypothetical point where the object would be if it was moving in a circular orbit with the same period as its true orbit after the same amount of time since it last crossed the perigee had elapsed.
argumentPerigee	Argument of perigee in radians. This is the angle between the direction of the ascending node and the direction of the perigee (the point of the orbit at which the object is closest to the Earth).

longitudeAscendingNode	Longitude of the ascending node (also called right ascension of the ascending node) in radians. This is the angle between the direction of the ascending node (the point where the satellite crosses the equatorial plane moving north) and the direction of the First Point of Aries (which indicates the location of the vernal equinox).
trueAnomaly	True anomaly of the orbit in radians. Unlike mean anomaly, true anomaly is the angle between the direction of the perigee and the actual position of the satellite.
argumentLatitude	Argument of latitude of the orbit in radians. Defined as the angle between the equator and the position of the satellite. It is useful to define the position of satellites in circular orbits, where the argument of perigee and true anomaly are not well defined.
longitudePerigee	Longitude of perigee of the orbit in radians. Defined as the angle between the vernal equinox and the perigee. It is useful for cases of orbits with 0 inclination, where the longitude of the ascending node and the argument of perigee are not well defined.
trueLongitude	Longitude of perigee of the orbit in radians. Defined as the angle between the vernal equinox and the position of the satellite. It is useful for cases of circular orbits with 0 inclination, where the longitude of the ascending node, the argument of perigee and true anomaly are not well defined.

References

<https://www.gsc-europa.eu/system-service-status/orbital-and-technical-parameters> <https://celestrak.org/columns/v02n01/>
https://www.faa.gov/about/office_org/headquarters_offices/avs/offices/aam/cami/library/online_libraries/aerospace_medicin

Examples

```
# The following were the position and velocity of satellite MOLNIYA 1-83
# the 25th of June, 2006 at 00:33:43 UTC in the GCRF frame (in m and m/s).

position_GCRF <- c(-14471729.582, -4677558.558, 9369.461)
velocity_GCRF <- c(-3251.691, -3276.008, 4009.228)

# Let's calculate the orbital elements of the satellite at that time

orbital_elements <- ECItokOE(position_GCRF, velocity_GCRF)
```

Description

The GCRF (Geocentric Celestial Reference Frame) frame of reference is an Earth-centered inertial coordinate frame, where the origin is placed at the center of mass of Earth and the coordinate frame is fixed with respect to the stars (and therefore not fixed with respect to the Earth surface in its rotation). The X-axis is aligned with the mean equinox of Earth at 12:00 Terrestrial Time on the 1st of January, 2000, and the Z-axis is aligned with the Earth's rotation axis.

It is almost equivalent to the J2000 frame of reference (also called EME2000), and in some contexts it is also referred to as ICRF frame (although in its strict definition, the origin of coordinates is placed at the barycenter of the Solar System).

In the ITRF (International Terrestrial Reference Frame), the origin is also placed at the center of mass of Earth, but the frame rotates with respect to the stars to remain fixed with respect to the Earth surface as it rotates. The Z-axis extends along the true North as defined by the IERS reference pole, and the X-axis extends towards the intersection between the equator and the Greenwich meridian at any time.

The coordinates and velocities input and calculated with the high-precision orbital propagator ([hpop](#)) are in the GCRF frame of reference.

This function requires the `asteRiskData` package, which can be installed by running `install.packages('asteRiskData', repos='https://rafael-ayala.github.io/drat/')`

Usage

```
GCRFtoITRF(position_GCRF, velocity_GCRF, dateTime)
```

Arguments

<code>position_GCRF</code>	Vector with the X, Y and Z components of the position of an object in GCRF frame, in m.
<code>velocity_GCRF</code>	Vector with the X, Y and Z components of the velocity of an object in GCRF frame, in m/s.
<code>dateTime</code>	Date-time string with the date and time in UTC corresponding to the provided position and velocity vectors. This specifies the time for which the conversion from GCRF to ITRF coordinates will be performed. It is important to provide an accurate value, since the point over the surface of Earth to which a set of GCRF coordinates refers varies with time due to the motion of Earth.

Value

A list with two elements representing the position and velocity of the satellite in the ITRF (International Terrestrial Reference Frame) frame of reference. Position values are in m, and velocity values are in m/s. Each of the two elements contains three values, corresponding to the X, Y and Z components of position and velocity in this order.

References

<https://celestrak.org/columns/v02n01/>

Examples

```

if(requireNamespace("asteRiskData", quietly = TRUE)) {
# The following were the position and velocity of satellite MOLNIYA 1-83
# the 25th of June, 2006 at 00:33:43 UTC in the GCRF frame (in m and m/s).

position_GCRF <- c(-14471729.582, -4677558.558, 9369.461)
velocity_GCRF <- c(-3251.691, -3276.008, 4009.228)

# Lets convert them into the ITRF frame

coordinates_ITRF <- GCRFtoITRF(position_GCRF, velocity_GCRF, "2006-06-27 00:58:29.34")
}

```

GCRFtoLATLON	<i>Convert coordinates from GCRF to geodetic latitude, longitude and altitude</i>
--------------	---

Description

The GCRF (Geocentric Celestial Reference Frame) frame of reference is an Earth-centered inertial coordinate frame, where the origin is placed at the center of mass of Earth and the coordinate frame is fixed with respect to the stars (and therefore not fixed with respect to the Earth surface in its rotation). The X-axis is aligned with the mean equinox of Earth at 12:00 Terrestrial Time on the 1st of January, 2000, and the Z-axis is aligned with the Earth's rotation axis. This function converts position in GCRF to geodetic latitude, longitude and altitude, which can be considered to be a non-inertial, Earth-centered frame of reference.

This function requires the `asteRiskData` package, which can be installed by running `install.packages('asteRiskData', repos='https://rafael-ayala.github.io/drat/')`

Usage

```
GCRFtoLATLON(position_GCRF, dateTime, degreesOutput=TRUE)
```

Arguments

position_GCRF	Vector with the X, Y and Z components of the position of an object in TEME frame, in m.
dateTime	Date-time string with the date and time in UTC corresponding to the provided position vector. This specifies the time for which the conversion from GCRF to geodetic coordinates will be performed. It is important to provide an accurate value, since the point over the surface of Earth to which a set of GCRF coordinates refers varies with time due to the motion of Earth.
degreesOutput	Logical indicating if the output should be in sexagesimal degrees. If <code>degreesOutput=FALSE</code> , the output will be in radians.

Value

A vector with three elements, corresponding to the latitude and longitude in degrees (or radians if specified) and the altitude in m.

References

<https://arc.aiaa.org/doi/10.2514/6.2006-6753>

Examples

```
if(requireNamespace("asteRiskData", quietly = TRUE)) {
# The following orbital parameters correspond to an object with NORAD catalogue
# number 24208 (Italsat 2) the 26th of June, 2006 at 00:58:29.34 UTC.

n0 <- 1.007781*((2*pi)/(1440)) # Multiplication by 2pi/1440 to convert to radians/min
e0 <- 0.002664 # mean eccentricity at epoch
i0 <- 3.8536*pi/180 # mean inclination at epoch in radians
M0 <- 48.3*pi/180 # mean anomaly at epoch in radians
omega0 <- 311.0977*pi/180 # mean argument of perigee at epoch in radians
OMEGA0 <- 80.0121*pi/180 # mean longitude of ascending node at epoch in radians
Bstar <- 1e-04 # drag coefficient
epochDateTime <- "2006-06-26 00:58:29.34"

# Lets calculate the position and velocity of the satellite 1 day later

state_1day_TEME <- sgdp4(n0=n0, e0=e0, i0=i0, M0=M0, omega0=omega0, OMEGA0=OMEGA0,
                        Bstar=Bstar, initialDateTime=epochDateTime, targetTime=1440)

# We can now convert the results in TEME frame to GCRF frame, previously
# multiplying by 1000 to convert the km output of sgdp4 to m

state_1day_GCRF <- TEMEtoGCRF(state_1day_TEME$position*1000,
                              state_1day_TEME$velocity*1000,
                              "2006-06-27 00:58:29.34")

# Finally, we convert the results in GCRF frame to geodetic latitude, longitude
# and altitude

state_1day_geodetic <- GCRFtoLATLON(state_1day_GCRF$position, "2006-06-27 00:58:29.34")
}
```

getLatestSpaceData *Retrieves the latest space data*

Description

The `asteRiskData` package provides the data and coefficients required for calculation of forces for `hpop` and other functions such certain conversions between reference frames. Some of the data tables included in the package are updated periodically with new data. These include Earth

orientation parameters, space weather data and solar and geomagnetic storms. In order to perform the calculations dependent on such data for the most recent times, the latest available data must be retrieved.

This function automatically updates the data tables, enabling such calculations for the most recent times.

Usage

```
getLatestSpaceData(targets="all")
```

Arguments

targets Character vector specifying the data that should be updated. It should be a vector containing one or more of the following strings: "all" (to update all data), "EOP" (Earth orientation parameters), "SW" (space weather), "SS" (solar storms) or "GS" (geomagnetic storms). By default, all data are updated.

Value

This function is invoked for its side effect, which is updating the data tables used internally for calculations requiring `asteRiskData` package, such as those performed by [hpop](#).

References

<http://www.celestrak.org/SpaceData/EOP-All.txt> <https://celestrak.org/SpaceData/SW-All.txt> <https://sol.spacenvironment.net>

Examples

```
if(interactive()) {
  if(requireNamespace("asteRiskData", quietly = TRUE)) {
    # The table of Earth orientation parameters distributed with asteRiskData
    # comprises data up to the 21st of March, 2021

    asteRiskData::earthPositions[nrow(asteRiskData::earthPositions),]

    # The table can be easily updated to include the most recent available data

    getLatestSpaceData(targets="all")
    asteRiskData::earthPositions[nrow(asteRiskData::earthPositions),]
  }
}
```

 hpop

High-precision numerical orbital propagator

Description

Given the position and velocity of a satellite at a given time (in the ICRF system of coordinates centered on the Solar System Barycenter, any of the main planets, Earth's Moon or Pluto), propagates its position by calculating its acceleration (based on a force model) and solving the resulting second-order ODE through numerical integration. This allows propagation of orbits with considerably higher accuracy than other propagators such as SGP4 and SDP4, but at the expense of a much higher computational cost. The forces and effects currently considered are gravitational attraction by the Earth (using the GGM05C gravity model, with spherical harmonics up to degree and order of 360); effects of Earth ocean and solid tides; gravitational attraction by the Moon (using the GRGM1200B gravity model with spherical harmonics up to degree and order of 1200), Sun and planets (considered as point masses); solar radiation pressure; atmospheric drag, and relativistic effects. The force-field is based on the forces described in *Satellite Orbits: Models, Methods and Applications* (Oliver Montenbruck and Eberhard Gill) and *Fundamentals of Astrodynamics and Applications* (David Vallado). The NRLMSISE-00 model is used to calculate atmospheric density for the calculation of atmospheric drag. The FES2014 model is used to calculate Earth geopotential model corrections due to ocean tides. As mentioned before, the central body for the frame of reference can be any of the Solar System Barycenter (SSB), any of the main planets, Earth's Moon or Pluto. By default, it is assumed to be Earth, corresponding to GCRF (Geocentric ICRF). The initial position will be checked against the position of said celestial bodies, to identify if it falls under the Laplacian gravitational sphere of influence of any of them. If this is the case, and it differs from the specified central body, the coordinate system will be changed to be centered on the celestial body whose sphere of influence includes the object of interest. This avoids instability in propagation. The high-precision numerical orbital propagator requires the `asteRiskData` package, which provides the data and coefficients required for calculation of the modeled forces. `asteRiskData` can be installed by running `install.packages('asteRiskData', repos='https://rafael-ayala.github.io/drat/')`

Usage

```
hpop(position, velocity, dateTime, times, satelliteMass, dragArea,
      radiationArea, dragCoefficient, radiationCoefficient,
      earthSphericalHarmonicsDegree=130, solidEarthTides=TRUE,
      oceanTides=TRUE, moonSphericalHarmonicsDegree=150, centralBody="Earth",
      autoCentralBodyChange=TRUE, ...)
```

Arguments

position	Initial position of the satellite in the GCRF system of coordinates. Should be provided as a numeric vector with 3 components that indicate the X, Y and Z components of the position in meters.
velocity	Initial velocity of the satellite in the GCRF system of coordinates. Should be provided as a numeric vector with 3 components that indicate the X, Y and Z components of the position in meters/second.

dateTime	Date time string in the YYYY-MM-DD HH:MM:SS format indicating the time corresponding to the initial position and velocity, in UTC time.
times	Vector with the times at which the position and velocity of the satellite should be calculated, in seconds since the initial time.
satelliteMass	Mass of the satellite in kilograms.
dragArea	Effective area of the satellite for atmospheric drag in squared meters. If the way that a satellite will orient with respect to its velocity is not known, a mean cross-sectional area should be calculated assuming that the orientation of the satellite with respect to its velocity will vary uniformly. A decent estimate can be obtained with a flat-plate model, where the satellite is considered to be parallelepiped-shaped. The mean effective area can then be calculated as $CSA = (S1 + S2 + S3 (+S4))/2$, where S1, S2 and S3 are the areas of the three perpendicular surfaces of the model and S4 is an optional term to account for the area of solar panels (potential masking between the solar panels and the main surfaces is not considered; this might be partially accounted for by introducing a factor to reduce the calculated effective area).
radiationArea	Effective area of the satellite subject to the effect of radiation pressure in squared meters.
dragCoefficient	Drag coefficient (Cd) used for the calculation of atmospheric drag. For low Earth-orbiting satellites, a value of 2.2 is frequently employed if a better approximation is not available.
radiationCoefficient	Coefficient for the force resulting from radiation pressure. This parameter is usually referred to as reflectivity coefficient (Cr) and the value varies for different satellites and orbits. If unknown, a value of 1.2 is usually a decent approximation.
earthSphericalHarmonicsDegree	Maximum degree and order that should be considered when calculating the Earth geopotential model. The model will be complete up to the specified degree/order, i.e., all zonal, sectorial and tesseral spherical harmonics will be calculated. The maximum possible value is 360, since that is the highest degree and order of the Stokes' coefficients provided in the GGM05C model. Note that spherical harmonics for Earth gravity field will only be used if Earth is the central body for propagation; otherwise, only a point-mass attraction will be calculated.
solidEarthTides	Logical indicating if corrections of the Cnm and Snm Stokes' coefficients for the geopotential model due to solid Earth tides should be performed, following IERS 2010 procedures and considering anelasticity of the Earth.
oceanTides	Logical indicating if corrections of the Cnm and Snm Stokes' coefficients for the geopotential model due to ocean tides should be performed, using the FES2014 oceanic tides model.
moonSphericalHarmonicsDegree	Maximum degree and order that should be considered when calculating the Moon gravity model. The model will be complete up to the specified degree/order, i.e., all zonal, sectorial and tesseral spherical harmonics will be calculated. The

maximum possible value is 1200, since that is the highest degree and order of the Stokes' coefficients provided in the GRGM1200B model. Note that spherical harmonics for Moon gravity field will only be used if Moon is the central body for propagation; otherwise, only a point-mass attraction will be calculated.

centralBody	Character string indicating the celestial body on which the supplied initial position (in ICRF) are centered. Should be one of "SSB" (meaning Solar System Barycenter), "Mercury", "Venus", "Earth", "Moon", "Mars", "Jupiter", "Saturn", "Uranus", "Neptune" or "Pluto". The initial position will be checked against the position of said celestial bodies, to identify if it falls under the Laplacian gravitational sphere of influence of any of them. If this is the case, and it differs from the specified central body, the coordinate system will be changed to be centered on the celestial body whose sphere of influence includes the object of interest.
autoCentralBodyChange	Logical indicating if the celestial object used as the center of coordinates should be automatically updated during propagation based on the radii of the spheres of influence of the main planets, the Moon and Pluto. By default, autoCentralBodyChange=TRUE.
...	Additional parameters to be passed to <code>ode</code> to control how numerical integration is performed. By default, the RADAU5 solver is used.

Value

A data frame with the results of the numerical integration at the requested times. Each row contains the results for one of the requested times. The data frame contains eight columns: time (indicating the time for the corresponding row in seconds since the initial time), X, Y, Z (indicating the X, Y and Z components of the position for that time in meters), dX, dY and dZ (indicating the X, Y and Z components of the velocity for that time in meters/second) and centralBody, indicating the central body of the frame of reference for the results for the corresponding time. Positions and velocities are returned in the ICRF frame of reference, centered in the celestial body specified in column centralBody. If autoCentralBodyChange=TRUE, the celestial body whose sphere of influence includes the object of interest will be automatically used as the central body. Additionally, if transitions in or out of the spheres of influence of the main celestial bodies are detected during propagation of the trajectory, the central body will be automatically modified accordingly. If autoCentralBodyChange=FALSE, such automatic changes of the central body will not be performed, and instead the user-specified central body will be used at all times. Note, however, that it is not recommended to perform propagation in a frame center at an object different than the celestial body whose sphere of influence includes the target of propagation, since this can lead to a substantial loss of accuracy. For details, see [M. Vautier, 2008](#). Note that, if none of the spheres of influence of the planets, Moon or Pluto included the object of interest, the center of the ICRF frame will be placed at the Solar System Barycenter.

References

Satellite Orbits: Models, Methods and Applications. Oliver Montenbruck and Eberhard Gill. Fundamentals of Astrodynamics and Applications. David Vallado. <https://www.mathworks.com/matlabcentral/fileexchange/5516-high-precision-orbit-propagator> <https://ccmc.gsfc.nasa.gov/modelweb/models/nrlmsise00.php> <https://digitalcommons.usu.edu/iopscience.iop.org/article/10.1088/1742-6596/911/1/012009/pdf> [https://www.sciencedirect.com/science/article/pii/S1674-6032\(08\)00034-1](https://www.sciencedirect.com/science/article/pii/S1674-6032(08)00034-1) https://etd.auburn.edu/bitstream/handle/10415/1133/Vautier_Manana_34.pdf?sequence=1

Examples

```

if(requireNamespace("asteRiskData", quietly = TRUE)) {
# The following are the position and velocity in the GCRF frame of satellite
# MOLNIYA 1-83 the 25th of June, 2006 at 00:33:43 UTC.

initialPosition <-c(-14568679.5026116, -4366250.78287623, 9417.9289105405)
initialVelocity <- c(-3321.17428902497, -3205.49400830455, 4009.26862308806)
initialTime <- "2006-06-25 00:33:43"

# Molniya satellites have a mass of approximately 1600 kg and a cross-section of
# 15 m2. Additionally, lets use 2.2 and 1.2 as approximately values of the
# drag and reflectivity coefficients, respectively.

molniyaMass <- 1600
molniyaCrossSection <- 15
molniyaCr <- 1.2
molniyaCd <- 2.2

# Lets calculate the position and velocity of the satellite for each minute of
# the following 10 minutes.

targetTimes <- seq(0, 600, by=60)
hpop_results <- hpop(initialPosition, initialVelocity, initialTime, targetTimes,
                    molniyaMass, molniyaCrossSection, molniyaCrossSection,
                    molniyaCr, molniyaCd)
}

```

ITRFtoGCRF

*Convert coordinates from ITRF to GCRF***Description**

The ITRF (International Terrestrial Reference Frame) is an ECEF (Earth Centered, Earth Fixed) frame of reference, i.e., a non-inertial frame of reference where the origin is placed at the center of mass of Earth, and the frame rotates with respect to the stars to remain fixed with respect to the Earth surface as it rotates. The Z-axis extends along the true North as defined by the IERS reference pole, and the X-axis extends towards the intersection between the equator and the Greenwich meridian at any time.

The GCRF (Geocentric Celestial Reference Frame) frame of reference is an Earth-centered inertial coordinate frame, where the origin is also placed at the center of mass of Earth and the coordinate frame is fixed with respect to the stars (and therefore not fixed with respect to the Earth surface in its rotation). The X-axis is aligned with the mean equinox of Earth at 12:00 Terrestrial Time on the 1st of January, 2000, and the Z-axis is aligned with the Earth's rotation axis.

This function requires the `asteRiskData` package, which can be installed by running `install.packages('asteRiskData', repos='https://rafael-ayala.github.io/drat/')`

Usage

```
ITRFtoGCRF(position_ITRF, velocity_ITRF, dateTime)
```

Arguments

position_ITRF	Vector with the X, Y and Z components of the position of an object in ITRF frame, in m.
velocity_ITRF	Vector with the X, Y and Z components of the velocity of an object in ITRF frame, in m/s.
dateTime	Date-time string with the date and time in UTC corresponding to the provided position and velocity vectors. This specifies the time for which the conversion from ITRF to GCRF coordinates will be performed. It is important to provide an accurate value, since the point over the surface of Earth to which a set of GCRF coordinates refers varies with time due to the motion of Earth.

Value

A list with two elements representing the position and velocity of the satellite in the GCRF (Earth-centered non-inertial) frame of reference. Position values are in m, and velocity values are in m/s. Each of the two elements contains three values, corresponding to the X, Y and Z components of position and velocity in this order.

References

<https://celestrak.org/columns/v02n01/>

Examples

```
if(requireNamespace("asteRiskData", quietly = TRUE)) {
# The following were the position and velocity of satellite MOLNIYA 1-83
# the 25th of June, 2006 at 00:33:43 UTC in the ECEF frame (in m and m/s).

position_ITRF <- c(1.734019e+06, -1.510972e+07, 39.08228)
velocity_ITRF <- c(1468.832, -3962.464, 4007.039)

# Lets convert them into the GCRF frame

coordinates_GCRF <- ITRFtoGCRF(position_ITRF, velocity_ITRF, "2006-06-25 00:33:43")
}
```

ITRFtoLATLON

Convert coordinates from ITRF to geodetic latitude, longitude and altitude

Description

The ITRF (International Terrestrial Reference Frame) is an ECEF (Earth Centered, Earth Fixed) frame of reference, i.e., a non-inertial frame of reference where the origin is placed at the center of mass of Earth, and the frame rotates with respect to the stars to remain fixed with respect to the Earth surface as it rotates. The Z-axis extends along the true North as defined by the IERS reference pole, and the X-axis extends towards the intersection between the equator and the Greenwich meridian at any time. This function converts Cartesian coordinates in the ECEF frame to geodetic latitude, longitude and altitude.

Usage

```
ITRFtoLATLON(position_ITRF, degreesOutput=TRUE)
```

Arguments

`position_ITRF` Vector with the X, Y and Z components of the position of an object in ITRF frame, in m.

`degreesOutput` Logical indicating if the output should be in sexagesimal degrees. If `degreesOutput=FALSE`, the output will be in radians.

Value

A vector with three elements, corresponding to the latitude and longitude in degrees (or radians if specified) and the altitude in m.

References

<https://arc.aiaa.org/doi/10.2514/6.2006-6753>

Examples

```
coordinates_ITRF <- c(5062040.1, -530657.4, 3863936.5)

# Let's calculate the geodetic latitude, longitude and altitude

geodetic <- ITRFtoLATLON <- (coordinates_ITRF)

# A longer application example follows, useful to represent the groundtrack of a
# satellite after propagation with SGP4/SDP4

if(requireNamespace("asteRiskData", quietly = TRUE)) {
  # The following orbital parameters correspond to an object with NORAD catalogue
  # number 24208 (Italsat 2) the 26th of June, 2006 at 00:58:29.34 UTC.

  n0 <- 1.007781*((2*pi)/(1440)) # Multiplication by 2pi/1440 to convert to radians/min
  e0 <- 0.002664 # mean eccentricity at epoch
  i0 <- 3.8536*pi/180 # mean inclination at epoch in radians
  M0 <- 48.3*pi/180 # mean anomaly at epoch in radians
  omega0 <- 311.0977*pi/180 # mean argument of perigee at epoch in radians
  OMEGA0 <- 80.0121*pi/180 # mean longitude of ascending node at epoch in radians
  Bstar <- 1e-04 # drag coefficient
  epochDateTime <- "2006-06-26 00:58:29.34"

  # Lets calculate the position and velocity of the satellite 1 day later

  state_1day_TEME <- sgdp4(n0=n0, e0=e0, i0=i0, M0=M0, omega0=omega0, OMEGA0=OMEGA0,
                          Bstar=Bstar, initialDateTime=epochDateTime, targetTime=1440)

  # We can now convert the results in TEME frame to ITRF frame, previously
  # multiplying by 1000 to convert the km output of sgdp4 to m
```

```

state_1day_ITRF <- TEMetoITRF(state_1day_TEME$position, state_1day_TEME$velocity,
                             "2006-06-27 00:58:29.34")

# Finally, we can convert the ECEF coordinates to geodetic latitude, longitude
# and altitude

state_1day_geodetic <- ITRFtoLATLON(state_1day_ITRF$position)
}

```

JPLEphemerides *Calculate JPL main celestial objects ephemerides for a given Modified Julian Date*

Description

NASA's Jet Propulsion Laboratory (JPL) provides mathematical models of the Solar System known as Development Ephemerides (DE). The models are given as sets of Chebyshev coefficients, which can be used to calculate the position (and its derivatives) of the Sun, the eight major planets, Pluto and the Moon. This function employs JPL DE440 to calculate the position (and optionally velocities also) of the mentioned celestial objects, in ICRF frame. JPL DE440 covers the period from 1550 to 2650 AC. In addition to the position of celestial objects, lunar libration angles are also calculated. Internally, calculations are performed by employing Clenshaw's algorithm together with the Chebyshev coefficients provided by JPL DE440. The target time should be specified as a Modified Julian Date (MJD). MJD in different time systems can be used. Currently, UTC, UT1, TT and TDB are supported. Additionally, a central body with respect to which positions and velocities are calculated should be specified. By default, the Solar System Barycenter (SSB) is used, but additionally Mercury, Venus, Earth, Moon, Mars, Jupiter, Saturn, Uranus, Neptune or Pluto can be selected. Note that this function requires the additional package `asteRiskData`, which provides the Chebyshev coefficients, and can be installed by running `install.packages("asteRiskData", repos="https://rafael-ayala.github.io/drat/")`

Usage

```
JPLEphemerides(MJD, timeSystem="UTC", centralBody="SSB", derivatives="acceleration")
```

Arguments

MJD	Modified Julian Date of the time for which celestial object ephemerides should be calculated. MJD are fractional number of days since midnight of the 17th of November, 1858. The MJD of a date-time string can be obtained with function dateTimeToMJD .
timeSystem	Time system into which the MJD is provided. Should be one from "UTC" (Coordinated Universal Time; default), "UT1" (Universal Time), "TT" (Terrestrial Time) and "TDB" (Barycentric Dynamical Time).
centralBody	String indicating the celestial object that will be taken as the center of coordinates to which positions and velocities are referred. Must be one of "SSB" (Solar System Barycenter), "Mercury", "Venus", "Earth", "Moon", "Mars", "Jupiter", "Saturn", "Uranus", "Neptune" or "Pluto".

derivatives String indicating what derivatives of positions should be calculated. Must be one of "none", "velocity" or "acceleration". If "none", only position is calculated. If "velocity", velocities are calculated, as well as first order derivatives of Moon libration angles. If "acceleration", both velocities and accelerations (as well as second order derivatives of Moon libration angles) are calculated.

Value

A list of vectors providing the positions (in meters), velocities (in m/s; only if requested), accelerations (in m/s²; only if requested), Moon libration angles (in radians), first derivatives of Moon libration angles (in radians/s; only if velocities were requested) and second derivatives of Moon libration angles (in radians/s²; only if accelerations were requested) of celestial objects with respect to the specified central body. For position, velocity and acceleration vectors, X, Y and Z components are given in this order. For Moon libration angles and their derivatives, they are given in the following order: phi, theta and psi.

References

https://gssc.esa.int/navipedia/index.php/Julian_Date https://gssc.esa.int/navipedia/index.php/Transformations_between_Tim

Examples

```
if(requireNamespace("asteRiskData", quietly = TRUE)) {
# Let's calculate the MJD of the 12th of June, 2000 at 10:00:00 UTC time, in UTC

MJD.UTC <- dateTimeToMJD("2000-06-12 10:00:00", timeSystem = "UTC")

# Let's now calculate the JPL ephemerides using Earth as the central body:

ephemerides <- JPLEphemerides(MJD.UTC, timeSystem = "UTC", centralBody="Earth")

# We can now calculate, for example, the exact distance between the barycenters
# of Earth and Moon

sqrt(sum(ephemerides$positionMoon^2))
}
```

KOtoECI

Calculate ECI coordinates from Keplerian orbital elements

Description

Keplerian orbital elements are a set of six parameters used to describe the orbits of celestial objects, including satellites. While satellites do not follow a perfectly Keplerian orbit, their state at any point can be defined by the orbital parameters that they would have if they were located at the same position with the same velocity following a perfectly Keplerian orbit (i.e., if perturbations were absent). These are called osculating orbital elements.

A complete set of six Keplerian elements defines unequivocally the position and velocity of the satellite in a given frame of reference, and therefore can be used to calculate its cartesian coordinates. This function calculates the coordinates of a satellite in an ECI (Earth-centered inertial) frame of reference from a set of Keplerian orbital elements. The exact ECI frame of the resulting coordinates is the same used to define the supplied orbital elements.

Usage

```
KOEtoECI(a, e, i, M, omega, OMEGA, keplerAccuracy=10e-8, maxKeplerIterations=100)
```

Arguments

a	Semi-major axis of orbital ellipse in meters.
e	Numerical eccentricity of the orbit. Eccentricity measures how much the orbit deviates from being circular.
i	Inclination of the orbital plane in radians. Inclination is the angle between the orbital plane and the equator.
M	Mean anomaly of the orbit in radians. Mean anomaly indicates where the satellite is along its orbital path, and is defined as the angle between the direction of the perigee and the hypothetical point where the object would be if it was moving in a circular orbit with the same period as its true orbit after the same amount of time since it last crossed the perigee had elapsed.
omega	Argument of perigee in radians. This is the angle between the direction of the ascending node and the direction of the perigee (the point of the orbit at which the object is closest to the Earth).
OMEGA	Right ascension of the ascending node in radians. This is the angle between the direction of the ascending node (the point where the satellite crosses the equatorial plane moving north) and the direction of the First Point of Aries (which indicates the location of the vernal equinox).
keplerAccuracy	Accuracy to consider Kepler's equation solved when calculating eccentric anomaly from mean anomaly. If two consecutive solutions differ by a value lower than this accuracy, integration is considered to have converged.
maxKeplerIterations	Maximum number of iterations after which fixed-point integration of Kepler's equation will stop, even if convergence according to the accuracy criterion has not been reached.

Value

A list with two elements representing the position and velocity of the satellite in the same ECI (Earth Centered, Earth Fixed) frame of reference into which the provided orbital elements were defined. Position values are in m, and velocity values are in m/s. Each of the two elements contains three values, corresponding to the X, Y and Z components of position and velocity in this order.

References

<https://www.gsc-europa.eu/system-service-status/orbital-and-technical-parameters> <https://celestrak.org/columns/v02n01/>
https://downloads.rene-schwarz.com/download/M001-Keplerian_Orbit_Elements_to_Cartesian_State_Vectors.pdf

Examples

```

# Let's calculate the ECI coordinates from the orbital elements provided by a
# TLE. It should be noted that this is often not recommended, since the orbital
# elements supplied in a TLE are not osculating orbital elements, but instead
# mean orbital elements set to fit a range of actual observations. The
# recommended procedures are to use TLE only in conjunction with the SGP4/SDP4
# models, and viceversa.
# The following orbital parameters correspond to an object with NORAD catalogue
# number 24208 (Italsat 2) the 26th of June, 2006 at 00:58:29.34 UTC.

n0 <- 1.007781*((2*pi)/(86400)) # Multiplication by 2pi/86400 to convert to radians/s
e0 <- 0.002664 # mean eccentricity at epoch
i0 <- 3.8536*pi/180 # mean inclination at epoch in radians
M0 <- 48.3*pi/180 # mean anomaly at epoch in radians
omega0 <- 311.0977*pi/180 # mean argument of perigee at epoch in radians
OMEGA0 <- 80.0121*pi/180 # mean longitude of ascending node at epoch in radians

# The semi-major axis can be calculated from the mean motion in radians/s
# as follows: (mu is the standard gravitational parameter of Earth)

mu <- 3.986004418e14 # in units of m3 s-2
a0 <- (mu^(1/3))/(n0^(2/3))

# The ECI coordinates can then be calculated. In this case, they will be in TEME
# frame, since the original orbital elements are derived from a TLE
coordinates_ECI <- KOEtoECI(a0, e0, i0, M0, omega0, OMEGA0)

```

LATLONtoGCRF

Convert coordinates from geodetic latitude, longitude and altitude to GCRF

Description

The GCRF (Geocentric Celestial Reference Frame) frame of reference is an Earth-centered inertial coordinate frame, where the origin is also placed at the center of mass of Earth and the coordinate frame is fixed with respect to the stars (and therefore not fixed with respect to the Earth surface in its rotation). The X-axis is aligned with the mean equinox of Earth at 12:00 Terrestrial Time on the 1st of January, 2000, and the Z-axis is aligned with the Earth's rotation axis. This function converts geodetic latitude, longitude and altitude to Cartesian coordinates in the GCRF frame. The WGS84 Earth ellipsoid model is used.

Usage

```
LATLONtoGCRF(position_LATLON, dateTime, degreesInput=TRUE)
```

Arguments

position_LATLON	Vector with the latitude, longitude and altitude of the object. Latitude and longitude can be provided in sexagesimal degrees or in radians (by default, sexagesimal degrees are assumed). Altitude must be provided in meters.
dateTime	Date-time string with the date and time in UTC corresponding to the provided geodetic coordinates.
degreesInput	Logical indicating if the input latitude and longitude are in sexagesimal degrees. If degreesInput=FALSE, the input will be considered to be in radians. This specifies the time for which the conversion from geodetic coordinates to GCRF will be performed. It is important to provide an accurate value, since the point over the surface of Earth to which a set of GCRF coordinates corresponds varies with time due to the motion of Earth.

Value

A vector with three elements, corresponding to the X, Y and Z components of position in meters in the ECEF frame, in this order.

References

<https://apps.dtic.mil/sti/pdfs/ADA280358.pdf>

Examples

```
if(requireNamespace("asteRiskData", quietly = TRUE)) {
  latitude <- 37.3891
  longitude <- -5.9845
  altitude <- 20000

  # Lets calculate the corresponding coordinates in GCRF frame, assuming that
  # the provided coordinates were valid the 20th of October, 2020 at 15:00:00 UTC

  coordinatesGCRF <- LATLONtoGCRF(c(latitude, longitude, altitude),
                                   dateTime="2020-10-20 15:00:00")
}
```

LATLONtoITRF

Convert coordinates from geodetic latitude, longitude and altitude to ITRF

Description

The ITRF (International Terrestrial Reference Frame) is an ECEF (Earth Centered, Earth Fixed) frame of reference, i.e., a non-inertial frame of reference where the origin is placed at the center of mass of Earth, and the frame rotates with respect to the stars to remain fixed with respect to the Earth surface as it rotates. The Z-axis extends along the true North as defined by the IERS reference pole,

and the X-axis extends towards the intersection between the equator and the Greenwich meridian at any time. This function converts geodetic latitude, longitude and altitude to Cartesian coordinates in the ITRF frame. The WGS84 Earth ellipsoid model is used.

Usage

```
LATLONtoITRF(position_LATLON, degreesInput=TRUE)
```

Arguments

position_LATLON	Vector with the latitude, longitude and altitude of the object. Latitude and longitude can be provided in sexagesimal degrees or in radians (by default, sexagesimal degrees are assumed). Altitude must be provided in meters.
degreesInput	Logical indicating if the input latitude and longitude are in sexagesimal degrees. If degreesInput=FALSE, the input will be considered to be in radians.

Value

A vector with three elements, corresponding to the X, Y and Z components of position in meters in the ITRF frame, in this order.

References

<https://apps.dtic.mil/sti/pdfs/ADA280358.pdf>

Examples

```
latitude <- 37.3891
longitude <- -5.9845
altitude <- 20000

# Lets calculate the corresponding coordinates in ECEF frame

coordinates_ITRF <- LATLONtoITRF(c(latitude, longitude, altitude))
```

parseTLElines

Parse the lines of a TLE

Description

TLE (Two-/Three- Line Element) is the standard format for representing orbital state vectors. This function parses a character vector where each element represents a line of the TLE. The supplied character vector can have either 2 (for Two Line Elements) or 3 (for Three Line Elements) elements. The two lines of a Two Line Element contain all the information. The additional line in a Three Line Element is optional, and contains just the satellite name. For a detailed description of the TLE format, see <https://celestrak.org/columns/v04n03/#FAQ01>.

Usage

```
parseTLElines(lines)
```

Arguments

lines Character vector where each element is a string corresponding to a line of the TLE. The character vector must have either 2 or 3 elements.

Value

A list with the following elements that define the orbital state vector of the satellite:

NORADcatalogNumber

NORAD Catalog Number, also known as Satellite Catalog Number, assigned by United States Space Command to each artificial object orbiting Earth

classificationLevel

Classification level of the information for the orbiting object. Can be unclassified, classified, secret or unknown

internationalDesignator

International Designator, also known as COSPAR ID, of the object. It consists of the launch year, separated by a hyphen from a three-digit number indicating the launch number for that year and a set of one to three letters indicating the piece for a launch with multiple pieces.

launchYear The launch year of the object

launchNumber The launch number of the object during its launch year

launchPiece The piece for the launch of the object, if it was a launch with multiple pieces

dateTime Date time string to which the orbital state vector corresponds

elementNumber Element number for the object. In principle, every time a new TLE is generated for an object, the element number is incremented, and therefore element numbers could be used to assess if all the TLEs for a certain object are available. However, in practice it is observed that this is not always the case, with some numbers skipped and some numbers repeated.

inclination Mean orbital inclination of the satellite in degrees. This is the angle between the orbital plane of the satellite and the equatorial plane

ascension Mean longitude of the ascending node of the satellite at epoch, also known as right ascension of the ascending node, in degrees. This is the angle between the direction of the ascending node (the point where the satellite crosses the equatorial plane moving north) and the direction of the First Point of Aries (which indicates the location of the vernal equinox)

eccentricity Mean eccentricity of the orbit of the object. Eccentricity is a measurement of how much the orbit deviates from a circular shape, with 0 indicating a perfectly circular orbit and 1 indicating an extreme case of parabolic trajectory

perigeeArgument

Mean argument of the perigee of the object in degrees. This is the angle between the direction of the ascending node and the direction of the perigee (the point of the orbit at which the object is closest to the Earth)

meanAnomaly	Mean anomaly of the orbit of the object in degrees. This indicates where the satellite is along its orbital path. It is provided as the angle between the direction of the perigee and the hypothetical point where the object would be if it was moving in a circular orbit with the same period as its true orbit after the same amount of time since it last crossed the perigee had elapsed. Therefore, 0 denotes that the object is at the perigee
meanMotion	Mean motion of the satellite at epoch in revolutions/day
meanMotionDerivative	First time derivative of the mean motion of the satellite in revolutions/day ²
meanMotionSecondDerivative	Second time derivative of the mean motion of the satellite in revolutions/day ³ .
Bstar	Drag coefficient of the satellite in units of (earth radii) ⁻¹ . Bstar is an adjusted value of the ballistic coefficient of the satellite, and it indicates how susceptible it is to atmospheric drag.
ephemerisType	Source for the ephemeris (orbital state vector). Most commonly, it is distributed data obtained by combining multiple observations with the SGP4/SDP4 models
epochRevolutionNumber	Number of full orbital revolutions completed by the object
objectName	Name of the object, retrieved from the first line of the TLE if a Three Line Element was provided

References

<https://celestrak.org/columns/v04n03/#FAQ01>

Examples

```
# The following lines correspond to a TLE for Italsat 2 the 26th of June, 2006
# at 00:58:29.34 UTC.
```

```
italsat2_lines <- c("ITALSAT 2",
"1 24208U 96044A 06177.04061740 -.00000094 00000-0 10000-3 0 1600",
"2 24208 3.8536 80.0121 0026640 311.0977 48.3000 1.00778054 36119")

italsat2_TLE <- parseTLElines(italsat2_lines)
italsat2_TLE
```

rad2deg *Converts an angle in radians to degrees*

Description

This function converts an angle in radians to degrees.

Usage

```
rad2deg(radians)
```

Arguments

radians Value of the angle in radians.

Value

The corresponding value of the angle in degrees.

Examples

```
rad2deg(pi)
```

```
readGLONASSNavigationRINEX
```

Read a RINEX navigation file for GLONASS satellites

Description

RINEX (Receiver Independent Exchange Format) is one of the most widely used formats for providing data of satellite navigation systems. The RINEX standard defines several structured text file types, among which navigation files are used to distribute positional information of the satellites. The exact information provided in a RINEX navigation file varies for each satellite navigation system. This function reads RINEX navigation files for satellites of the GLONASS constellation, operated by Russia.

Usage

```
readGLONASSNavigationRINEX(filename)
```

Arguments

filename Path to the GLONASS RINEX navigation file.

Value

A list with two elements. The first element, named header, is a list with the following elements:

rinexVersion	Version of the RINEX format used in the file
rinexFileType	Type of RINEX file
generatorProgram	Program used to generate the RINEX file
generatorEntity	Individual or organization that generated the file
fileCreationDateString	Date-time string indicating when the file was created
refYear	Reference year for system time correction
refMonth	Reference month for system time correction

refDay	Reference day for system time correction
sysTimeCorrection	Correction to system time scale to fine-tune GLONASS time to UTC in seconds. Since GLONASS time is linked to UTC, it should be a very small amount
leapSeconds	Leap seconds introduced since 1980. Useful to convert to GPS time
comments	Miscellaneous comments found in the header of the RINEX file

The second element is named messages, and it contains one element for each navigation message found in the RINEX file. Each of these elements is a list with the following elements that provide information about the position of the GLONASS satellite:

satelliteNumber	Slot number of the satellite within the GLONASS constellation. It can be converted to a PRN code by adding 37 to it
epochYearShort	Epoch year in 2-digit format. If lower than 80, the meaning should be taken as 20XX, while if larger than 80, it refers to 19XX.
epochMonth	Epoch month
epochDay	Epoch day
epochHour	Epoch hour
epochMinute	Epoch minute
epochSecond	Epoch second
ephemerisUTCTime	A nanotime object indicating the time corresponding to the reported position (ephemeris) in the present message. The time is in UTC, obtained by applying the individual clock bias of the particular satellite (clockBias field of each message) and the latest global GLONASS time bias with respect to UTC (sysTimeCorrection field of the header) to the uncorrected ephemeris time, given by the previous time fields. Corrections are performed as described in the GLONASS system specifications (https://russianspacesystems.ru/wp-content/uploads/2016/08/ICD_GLONASS_eng_v5.1.pdf)
clockBias	Clock bias (i.e., constant offset) that should be applied to the satellite time in order to obtain an even more accurate UTC time. In seconds
relativeFreqBias	Clock drift of the satellite clock that should be applied in combination with the time difference to the reference time in order to obtain an even more accurate UTC time. In seconds per second
messageFrameTime	Second of the UTC day when the message was transmitted
positionX	X coordinate of the position of the satellite in km, in the ITRF system of coordinates
positionY	Y coordinate of the position of the satellite in km, in the ITRF system of coordinates
positionZ	Z coordinate of the position of the satellite in km, in the ITRF system of coordinates

velocityX	X component of the velocity of the satellite in km/s, in the ITRF system of coordinates
velocityY	Y component of the velocity of the satellite in km/s, in the ITRF system of coordinates
velocityZ	Z component of the velocity of the satellite in km/s, in the ITRF system of coordinates
accelX	X component of the accel of the satellite in km/s, in the ITRF system of coordinates
accelY	Y component of the accel of the satellite in km/s, in the ITRF system of coordinates
accelZ	Z component of the accel of the satellite in km/s, in the ITRF system of coordinates
satelliteHealthCode	Code indicating the health of the satellite. 0 if healthy
freqNumber	Frequency number (k) of the GLONASS satellite. The two frequencies in MHz, f1 and f2, used by the satellite to transmit data can be calculated as follows: $f1 = 1602 + k*9/16$ and $f2 = 1246 + k*7/16$
informationAge	Age in days of the observation data used to generate the provided ephemeris

References

<https://gage.upc.edu/gFD/> <https://www.navcen.uscg.gov/pubs/gps/rinex/rinex.txt> <ftp://www.ngs.noaa.gov/cors/RINEX211.txt>
<http://acc.igs.org/misc/rinex304.pdf> https://russianspacesystems.ru/wp-content/uploads/2016/08/ICD_GLONASS_eng_v5.1

Examples

```
# The file testGLONASSRINEX.txt provided with the package includes 5 navigation
# messages from 4 GLONASS satellites

testGLONASSnav <- readGLONASSNavigationRINEX(paste0(path.package("asterisk"),
"/testGLONASSRINEX.txt"))
testGLONASSnav$header
testGLONASSnav$messages
```

```
readGPSNavigationRINEX
```

Read a RINEX navigation file for GPS satellites

Description

RINEX (Receiver Independent Exchange Format) is one of the most widely used formats for providing data of satellite navigation systems. The RINEX standard defines several structured text file types, among which navigation files are used to distribute positional information of the satellites. The exact information provided in a RINEX navigation file varies for each satellite navigation system. This function reads RINEX navigation files for satellites of the GPS constellation, operated by the USA.

Usage

```
readGPSNavigationRINEX(filename)
```

Arguments

filename Path to the GPS RINEX navigation file.

Value

A list with two elements. The first element, named header, is a list with the following elements:

rinexVersion	Version of the RINEX format used in the file
rinexFileType	Type of RINEX file
generatorProgram	Program used to generate the RINEX file
generatorEntity	Individual or organization that generated the file
fileCreationDateString	Date-time string indicating when the file was created
ionAlphaA0	Coefficient for ionospheric correction A0
ionAlphaA1	Coefficient for ionospheric correction A1
ionAlphaA2	Coefficient for ionospheric correction A2
ionAlphaA3	Coefficient for ionospheric correction A3
ionBetaB0	Coefficient for ionospheric correction B0
ionBetaB1	Coefficient for ionospheric correction B1
ionBetaB2	Coefficient for ionospheric correction B2
ionBetaB3	Coefficient for ionospheric correction B3
deltaUTCA0	A0 parameter, corresponding to bias between GPST and UTC time at the reference time (Tot) given by fields referenceTimeUTC and referenceWeekUTC. Should be used to compute accurate time in UTC
deltaUTCA1	A1 parameter, corresponding to the clock drift between GPST and UTC at the reference time (Tot) given by fields referenceTimeUTC and referenceWeekUTC. Should be used to compute accurate time in UTC
referenceTimeUTC	Time in seconds of current UTC week of Tot, which is the reference time to correct GPST time to UTC
referenceWeekUTC	UTC reference week number (continuous scale, not modulo 1024) of Tot.
leapSeconds	Leap seconds introduced since the 6th of January, 1980. Useful to convert to UTC time (UTC time = GPS time - leap seconds)
comments	Miscellaneous comments found in the header of the RINEX file

The second element is named messages, and it contains one element for each navigation message found in the RINEX file. Each of these elements is a list with the following elements that provide information about the position of the GPS satellite:

satellitePRNCode	PRN code of the satellite. Unique PRN codes are assigned to all satellites in global navigation satellite systems, and therefore provide an identifier for each of them
tocYearShort	Toc year in 2-digit format. If lower than 80, the meaning should be taken as 20XX, while if larger than 80, it refers to 19XX. Toc is the GPS time of the specific satellite that should be used as the time reference to apply clock bias, clock drift and possibly even clock drift rate, as well as a relativistic correction, as described in the GPS system specification (https://www.gps.gov/technical/icwg/IS-GPS-200H.pdf) to obtain the corrected GPST system time. The GPST system time can be converted to UTC time by subtracting leap seconds since the 6th of January 1980 and performing another polynomial correction to account for bias and drift between GPST and UTC times.
tocMonth	Toc month
tocDay	Toc day
tocHour	Toc hour
tocMinute	Toc minute
tocSecond	Toc second
UTCepochDateTime	Date-time string indicating the time corresponding to the reported position in the present message. The time is in UTC, obtained by subtracting the leap seconds (if available in the header) from the time of the satellite system (which is in GPS time). If leap seconds are not provided in the header, the time will be in GPS. For an even more accurate conversion to actual UTC time, the clock bias, clock drift and possibly even clock drift rate (described in the next three elements) must be considered
clockBias	Clock bias (i.e., constant offset) at Toc that should be applied to the satellite time in order to calculate accurate GPST. In seconds. Often referred to as af0.
clockDrift	Clock drift of the satellite clock at Toc that should be applied to the satellite time in order to calculate accurate GPST. In seconds. Often referred to as af1.
clockDriftRate	Rate of change for the clock drift of the satellite clock at Toc. It is frequently 0, but if not, it should be applied in combination with clock bias and clock drift in order to correct to GPST as accurately as possible. In seconds per square second. Often referred to as af2.
IODE	Issue-of-data ephemeris. It acts as a time-stamp or unique identifier for the provided navigation data. In particular, the IODE of a given navigation message should never be the same as the IODE for any other navigation message broadcasted by the same satellite in the past 6 days, although violations of this rule have been observed. Most frequently, IODE are not reused in a period of 7 days, so that they match exactly the IODC.
radiusCorrectionSine	Amplitude of the sine harmonic component for the correction of orbital radius. In meters
deltaN	Mean motion difference from computed value. In radians per second. In order to obtain the real (perturbed) mean motion, first the Keplerian mean motion should be calculated from the semi-major axis. Then, deltaN should be added to it.

correctedMeanMotion	Corrected mean motion calculated by adding deltaN to the value computed from the semi-major axis. In radians per second
meanAnomaly	Mean anomaly of the satellite at epoch. In radians. This indicates where the satellite is along its orbital path. It is provided as the angle between the direction of the perigee and the hypothetical point where the object would be if it was moving in a circular orbit with the same period as its true orbit after the same amount of time since it last crossed the perigee had ellapsed. Therefore, 0 denotes that the object is at the perigee. This is a Keplerian orbital element.
latitudeCorrectionCosine	Amplitude of the cosine harmonic component for the correction of latitude argument. In radians
eccentricity	Eccentricity of the orbit of the satellite at epoch. This is a Keplerian orbital element.
latitudeCorrectionSine	Amplitude of the sine harmonic component for the correction of latitude argument. In radians
semiMajorAxis	Semi-major axis of the orbit of the satellite at epoch. In meters. This is a Keplerian orbital element
toeSecondsOfGPSWeek	Time of the GPS week (in seconds) for the ephemeris. Together with the toeGPSWeek, it can be used to calculate the ephemeris time in GPS time of the specific satellite, to which sequential corrections first to GPST and then to UTC should be applied.
inclinationCorrectionCosine	Amplitude of the cosine harmonic component for the correction of inclination. In radians
ascension	Longitude of the ascending node of the satellite at epoch, also known as right ascension of the ascending node, in radians. This is the angle between the direction of the ascending node (the point where the satellite crosses the equatorial plane moving north) and the direction of the First Point of Aries (which indicates the location of the vernal equinox). This is a Keplerian orbital element.
inclinationCorrectionSine	Amplitude of the sine harmonic component for the correction of inclination. In radians
inclination	Mean orbital inclination of the satellite in radians. This is the angle between the orbital plane of the satellite and the equatorial plane. This is a Keplerian orbital element.
radiusCorrectionCosine	Amplitude of the cosine harmonic component for the correction of orbital radius. In meters.
perigeeArgument	Mean argument of the perigee of the object in radians. This is the angle between the direction of the ascending node and the direction of the perigee (the point of the orbit at which the object is closest to the Earth). This is a Keplerian orbital element.

OMEGADot	Angular velocity of the satellite with respect to the vernal equinox. In radians/second.
codesL2Channel	Flag indicating if coarse/acquisition (C/A) code is being transmitted on the L2 channel (value of 1) or not (value of 0)
toeGPSWeek	GPS week number at epoch
dataFlagL2P	Flag indicating if precise (P) code is being transmitted on the L2 channel (value of 1) or not (value of 0)
satelliteAccuracy	Accuracy of the position of the satellite, in meters.
satelliteHealthCode	Code indicating the health of the satellite. 0 if healthy.
totalGroupDelay	Bias difference between codes broadcasted on L1 and the ionospheric-free combination of the codes broadcasted at L1 and L2, in seconds. This parameter, also known as timing group delay (TGD), should be considered when calculating satellite clock error.
IODC	Issue-of-data clock. It acts as a time-stamp or unique identifier for the provided navigation data. In particular, the IODC of a given navigation message should never be the same as the IODC for any other navigation message broadcasted by the same satellite in the past 7 days, although violations of this rule have been observed. Most frequently, IODE are not reused in a period of 7 days instead of the mandatory 6 days, so that they match exactly the IODC.
transmissionTime	Transmission time for the navigation message, in seconds of GPS week.
fitInterval	Flag indicating for how long the broadcasted ephemeris are valid since the last time the data was updated. It should be noted that in order to obtain positional values/orbital elements at times other than epoch, the corrections for perturbed orbital elements should be applied and propagated. If 0, the ephemeris data are valid for up to 4 hours. If 1, they are valid for more than 4 hours.
ephemerisUTCTime	A nanotime object indicating the time corresponding to the reported position (ephemeris) in the present message. The time is in UTC, obtained by first applying the individual clock bias, clock drift and clock drift rate of the particular satellite (fields <code>clockBias</code> , <code>clockDrift</code> and <code>clockDriftRate</code> of each message) and a relativistic correction to obtain corrected GPST time (system-wide GPS time), and then subtraction of leap seconds since the 6th of January 1980 and a second polynomial correction (with fields <code>deltaUTCA0</code> and <code>deltaUTCA1</code> from the header) to obtain UTC time. Corrections are performed as described in the GPS system specifications (https://www.gps.gov/technical/icwg/IS-GPS-200H.pdf).
position_ITRF	Position of the satellite in the ITRF frame, calculated from the provided orbital ephemeris following the procedure described in the GPS system specifications. In meters.
velocity_ITRF	Velocity of the satellite in the ITRF frame, calculated from the provided orbital ephemeris following the procedure described in the GPS system specifications. In meters/second.

acceleration_ITRF

Acceleration of the satellite in the ITRF frame, calculated from the provided orbital ephemeris following the procedure described in the GPS system specifications. In meters/squared second.

References

<https://gage.upc.edu/gFD/> <https://www.navcen.uscg.gov/pubs/gps/rinex/rinex.txt> <ftp://www.ngs.noaa.gov/cors/RINEX211.txt>
<http://acc.igs.org/misc/rinex304.pdf> <https://www.icao.int/Meetings/AMC/MA/2004/GNSS/icd.pdf> <https://www.gps.gov/tech/GPS-200H.pdf>

Examples

```
# The file testGPSRINEX.txt provided with the package includes 3 navigation
# messages from 3 GPS satellites
```

```
testGPSnav <- readGPSNavigationRINEX(paste0(path.package("asterisk"),
"/testGPSRINEX.txt"))
testGPSnav$header
testGPSnav$messages
```

readOEM

Read an Orbital Ephemeris Message file

Description

OEM (Orbital Ephemeris Message) is one of the three standard file formats defined by the CCSDS for transferring spacecraft orbit information. OEM files contain the position and velocity of a given object at multiple times (epochs). They can also contain optionally acceleration values, covariance matrixes that indicate the uncertainty of the provided state vectors and other additional information. This function reads OEM files, retrieving also the optional fields.

Usage

```
readOEM(filename)
```

Arguments

filename Path to the OEM file.

Value

A list with two elements. The first element, named header, is a list with the following elements:

OMVersion	Version of the OEM format used in the file
creationDate	Date of creation of the file
creator	Individual or organization that generated the file

The second element is named `dataBlocks`, and it contains one element for each ephemeris data block found in the OEM file. Each of these elements is a list with the following elements that provide information about the ephemerides of object (note that some elements are not mandatory and therefore might not be present in all OEM files; in these cases, their value is set to NULL):

<code>objectName</code>	Name of the object
<code>objectID</code>	Object identifier for the object. Frequently, although not always, the identifier has the format YYYY-NNNPPP, where YYYY is the year of launch, NNN is the three-digit serial number specifying the launch number during year YYYY and PPP is a part specifier comprising 1 to 3 capital letters that indicate the part of the object put into space during the launch.
<code>referenceFrame</code>	Frame of reference in which ephemerides are provided.
<code>refFrameEpoch</code>	Epoch for the frame of reference, for cases where it is not intrinsic to the frame itself, such as TEME.
<code>centerName</code>	Name of the center of coordinates. For example, a celestial body, the barycenter of the entire Solar System or even other spacecraft.
<code>timeSystem</code>	Time system used for the ephemerides, covariance matrixes and all other time fields of the data block.
<code>startTime</code>	Start time of the time span covered by the ephemerides and covariance matrixes in this data block.
<code>endTime</code>	End time of the time span covered by the ephemerides and covariance matrixes in this data block.
<code>usableStartTime</code>	Start time of the usable time span covered by the ephemerides and covariance matrixes in this data block.
<code>usableEndTime</code>	End time of the usable time span covered by the ephemerides and covariance matrixes in this data block.
<code>interpolationMethod</code>	Recommended interpolation method to calculate ephemerides at epochs between those directly given in the data block.
<code>interpolationOrder</code>	Recommended interpolation degree to calculate ephemerides at epochs between those directly given in the data block.
<code>mass</code>	Mass in kg of the object.
<code>dragArea</code>	Effective area of the object subjected to drag, in square meters.
<code>dragCoefficient</code>	Drag coefficient of the object.
<code>solarRadArea</code>	Effective area of the object subjected to solar radiation pressure, in square meters.
<code>solarRadCoefficient</code>	Solar radiation pressure coefficient of the object.
<code>ephemerides</code>	Data frame with the 7 or 10 columns providing the ephemerides for the object. The 1st column provides the epochs for each ephemeris; columns 2 to 4 provide the X, Y and Z components of position (in km), and columns 5 to 7 provide the X, Y and Z components of velocity (in km/s). Columns 8 to 10 are optional, and if present provide the X, Y and Z components of acceleration (in km/s ²)

covarianceMatrixes

List where each element is a 3-element list that provides a covariance matrix for this data block. Each of the 3-element lists corresponding to a covariance matrix contains the following elements:

- epoch Epoch of the navigation solution related to this covariance matrix.
- referenceFrame Reference frame for the covariance matrix. Frequently this is the same as for the ephemerides. In order to facilitate interpretation of the covariance matrix, conversion to a perifocal frame of reference might be advisable.
- covarianceMatrix Covariance matrix that provides information about the uncertainties of position and velocities. This is a symmetric 6x6 matrix where the values in the diagonal are the squared standard deviations of each variable, and the other values are covariances between 2 variables (those corresponding to the row and column of each value). The rows and columns correspond to the following variables, in the specified order: X position, Y position, Z position, X velocity, Y velocity and Z velocity.

References

<https://public.ccsds.org/Pubs/502x0b2c1e2.pdf> https://spotthestation.nasa.gov/trajectory_data.cfm

Examples

```
# The file testOEM.txt provided with the package includes ephemerides data
# for the ISS publicly available

testOEM_ISS <- readOEM(paste0(path.package("asteRisk"), "/testOEM.txt"))
testOEM_ISS$header
testOEM_ISS$dataBlocks[[1]]$objectName
head(testOEM_ISS$dataBlocks[[1]]$ephemerides)
```

readTLE

Read a TLE file

Description

TLE (Two-/Three- Line Element) is a standard structured text file format for representing orbital state vectors. This function reads a TLE file containing one or more TLEs. The TLE file can contain either Two Line Elements or Three Line Elements, but all the TLE in a single file must be of the same type. The two lines of a Two Line Element contain all the ephemeris information. The additional line in a Three Line Element is optional, and contains just the satellite name. For a detailed description of the TLE format, see <https://celestrak.com/columns/v04n03/#FAQ01>.

Usage

```
readTLE(filename, maxTLEs=NULL)
```

Arguments

filename	Path to the TLE file. Alternatively, an URL pointing to a TLE file.
maxTLEs	Maximum number of TLEs to read, starting from the beginning of the file. By default, all TLEs present in the file are read.

Value

A list with the following elements that define the orbital state vector of the satellite (or, if the file contained multiple TLE, a nested list, where each element of the top level list represents an orbital state vector, and comprises the following elements):

NORADcatalogNumber	NORAD Catalog Number, also known as Satellite Catalog Number, assigned by United States Space Command to each artificial object orbiting Earth
classificationLevel	Classification level of the information for the orbiting object. Can be unclassified, classified, secret or unknown
internationalDesignator	International Designator, also known as COSPAR ID, of the object. It consists of the launch year, separated by a hyphen from a three-digit number indicating the launch number for that year and a set of one to three letters indicating the piece for a launch with multiple pieces.
launchYear	The launch year of the object
launchNumber	The launch number of the object during its launch year
launchPiece	The piece for the launch of the object, if it was a launch with multiple pieces
dateTime	Date time string to which the orbital state vector corresponds
elementNumber	Element number for the object. In principle, every time a new TLE is generated for an object, the element number is incremented, and therefore element numbers could be used to assess if all the TLEs for a certain object are available. However, in practice it is observed that this is not always the case, with some numbers skipped and some numbers repeated.
inclination	Mean orbital inclination of the satellite in degrees. This is the angle between the orbital plane of the satellite and the equatorial plane
ascension	Mean longitude of the ascending node of the satellite at epoch, also known as right ascension of the ascending node, in degrees. This is the angle between the direction of the ascending node (the point where the satellite crosses the equatorial plane moving north) and the direction of the First Point of Aries (which indicates the location of the vernal equinox)
eccentricity	Mean eccentricity of the orbit of the object. Eccentricity is a measurement of how much the orbit deviates from a circular shape, with 0 indicating a perfectly circular orbit and 1 indicating an extreme case of parabolic trajectory
perigeeArgument	Mean argument of the perigee of the object in degrees. This is the angle between the direction of the ascending node and the direction of the perigee (the point of the orbit at which the object is closest to the Earth)

meanAnomaly	Mean anomaly of the orbit of the object in degrees. This indicates where the satellite is along its orbital path. It is provided as the angle between the direction of the perigee and the hypothetical point where the object would be if it was moving in a circular orbit with the same period as its true orbit after the same amount of time since it last crossed the perigee had elapsed. Therefore, 0 denotes that the object is at the perigee
meanMotion	Mean motion of the satellite at epoch in revolutions/day
meanMotionDerivative	First time derivative of the mean motion of the satellite in revolutions/day ²
meanMotionSecondDerivative	Second time derivative of the mean motion of the satellite in revolutions/day ³ .
Bstar	Drag coefficient of the satellite in units of (earth radii) ⁻¹ . Bstar is an adjusted value of the ballistic coefficient of the satellite, and it indicates how susceptible it is to atmospheric drag.
ephemerisType	Source for the ephemeris (orbital state vector). Most commonly, it is distributed data obtained by combining multiple observations with the SGP4/SDP4 models
epochRevolutionNumber	Number of full orbital revolutions completed by the object
objectName	Name of the object, retrieved from the first line of the TLE if a Three Line Element was provided

References

<https://celestrak.org/columns/v04n03/#FAQ01> <http://www.celestrak.org/publications/aiaa/2006-6753/AIAA-2006-6753.pdf>

Examples

```
# The file testTLE.txt provided with the package includes 29 TLE covering a
# variety of satellites, extracted from Revisiting Space Track Report #3

test_TLEs <- readTLE(paste0(path.package("asterisk"), "/testTLE.txt"))
test_TLEs
```

revDay2radMin	<i>Converts revolutions per day to radians per minute</i>
---------------	---

Description

This function converts a rotation rate in revolutions per day to radians per minute. This conversion is useful since values in TLEs are given in revolutions per day, but the SGP4 and SDP4 propagators require the mean motion to be provided in radians per minute.

Usage

```
revDay2radMin(revPerDay)
```

Arguments

revPerDay Value of the rotation rate in revolutions per day.

Value

The corresponding value of the rotation rate in radians per minute.

Examples

```
revDay2radMin(2)
```

sdp4

Propagate an orbital state vector with the SDP4 model

Description

Given an orbital state vector of a satellite, applies the SDP4 model to propagate its orbit to the desired time point. This allows the calculation of the position and velocity of the satellite at different times, both before and after the time corresponding to the known state vector (referred to as "epoch"). Kepler's equation is solved through fixed-point integration. The SDP4 model is a modified version of the SGP4 model that takes into account the secular and periodic perturbations of the Moon and the Sun on the orbit of the satellite. It also considers the Earth resonance effects on 24-hour geostationary and 12-hour Molniya orbits. Thanks to this, the SDP4 model can correctly propagate the orbit of objects in deep space (with orbital periods larger than 225 minutes, corresponding to altitudes higher than 5877.5 km). However, it should be noted that SDP4 employs only simplified drag equations, and lacks corrections for low-perigee orbits. Therefore, it is recommended to apply the standard SGP4 model (available through the [sgp4](#) function) for satellites that are not in deep space. This implementation is based on a previous SDP4 implementation in Julia (SatelliteToolbox).

Usage

```
sdp4(n0, e0, i0, M0, omega0, OMEGA0, Bstar, initialDateTime, targetTime,
    keplerAccuracy=10e-12, maxKeplerIterations=10)
```

Arguments

n0 Mean motion of the satellite at epoch in radians/min.

e0 Mean eccentricity of the orbit of the satellite at epoch. Eccentricity ranges from 0 (perfectly circular orbit) to 1 (parabolic trajectory).

i0 Mean orbital inclination of the satellite at epoch in radians.

M0 Mean anomaly of the satellite at epoch.

omega0 Mean argument of perigee of the satellite at epoch.

OMEGA0 Mean longitude of the ascending node of the satellite at epoch. Also known as right ascension of the ascending node.

Bstar	Drag coefficient of the satellite in units of (earth radii) ⁻¹ . Bstar is an adjusted value of the ballistic coefficient of the satellite, and it indicates how susceptible it is to atmospheric drag.
initialDateTime	Date-time string in UTC indicating the time corresponding to the known state vector of the satellite. Unlike for SGP4, it must be provided in all cases since it is required to calculate Moon and Sun perturbations.
targetTime	Time at which the position and velocity of the satellite should be calculated. It can be provided in two different ways: either as a number corresponding to the time in minutes counting from epoch at which the orbit should be propagated, or as a date-time string in UTC.
keplerAccuracy	Accuracy to consider Kepler's equation solved. If two consecutive solutions differ by a value lower than this accuracy, integration is considered to have converged.
maxKeplerIterations	Maximum number of iterations after which fixed-point integration of Kepler's equation will stop, even if convergence according to the accuracy criterion has not been reached.

Value

A list with three elements. The first two elements represent the position and velocity of the satellite at the target time, in the TEME (True Equator, Mean Equinox) frame of reference. Position values are in km, and velocity values are in km/s. Each of these two elements contains three values, corresponding to the X, Y and Z components of position and velocity in this order. The third element indicates the algorithm used to propagate the orbit (sdp4).

References

<https://juliapackages.com/p/satellittoolbox> <https://celestrak.org/NORAD/documentation/spacetrk.pdf>
<http://www.celestrak.org/publications/aiaa/2006-6753/AIAA-2006-6753.pdf>

Examples

```
# The following orbital parameters correspond to an object with NORAD catalogue
# number 24208 (Italsat 2) the 26th of June, 2006 at 00:58:29.34 UTC.

n0 <- 1.007781*((2*pi)/(1440)) # Multiplication by 2pi/1440 to convert to radians/min
e0 <- 0.002664 # mean eccentricity at epoch
i0 <- 3.8536*pi/180 # mean inclination at epoch in radians
M0 <- 48.3*pi/180 # mean anomaly at epoch in radians
omega0 <- 311.0977*pi/180 # mean argument of perigee at epoch in radians
OMEGA0 <- 80.0121*pi/180 # mean longitude of ascending node at epoch in radians
Bstar <- 1e-04 # drag coefficient
epochDateTime <- "2006-06-26 00:58:29.34"

# Calculation of the orbital period

2*pi/n0
```

```

# The period is higher than 225 min, and therefore the SDP4 model should be
# applied. Furthermore, from the mean motion in revolutions/day, it can be
# seen that it is a geostationary satellite with a 24-hour period. Lets
# calculate and compare the position and velocity of the satellite at epoch
# and 1 day later.

state_0 <- sdp4(n0=n0, e0=e0, i0=i0, M0=M0, omega0=omega0, OMEGA0=OMEGA0,
               Bstar=Bstar, initialDateTime=epochDateTime, targetTime=0)
state_1day <- sdp4(n0=n0, e0=e0, i0=i0, M0=M0, omega0=omega0, OMEGA0=OMEGA0,
                  Bstar=Bstar, initialDateTime=epochDateTime, targetTime=1440)

state_0
state_1day

# The position and velocity are very similar after a full day, in accordance
# with the geostationary orbit

```

sgdp4

Propagate an orbital state vector with the SGP4/SDP4 model

Description

Given an orbital state vector of a satellite, applies the SGP4 or SDP4 model to propagate its orbit to the desired time point, as appropriate depending on the orbital period. The model will be automatically chosen depending on the orbital period. For objects in deep space (with orbital periods larger than 225 minutes, equivalent to altitudes higher than 5877.5 km) the SDP4 model will be applied. For objects near Earth (orbital periods shorter than 225 minutes, or altitudes lower than 5877.5 km) the SGP4 model will be used. It is not recommended to apply SGP4 to objects in deep space or SDP4 to objects near Earth, but this can be forced by calling directly the [sgp4](#) and [sdp4](#) functions.

Usage

```
sgdp4(n0, e0, i0, M0, omega0, OMEGA0, Bstar, initialDateTime=NULL, targetTime,
      keplerAccuracy=10e-12, maxKeplerIterations=10)
```

Arguments

n0	Mean motion of the satellite at epoch in radians/min.
e0	Mean eccentricity of the orbit of the satellite at epoch. Eccentricity ranges from 0 (perfectly circular orbit) to 1 (parabolic trajectory).
i0	Mean orbital inclination of the satellite at epoch in radians.
M0	Mean anomaly of the satellite at epoch.
omega0	Mean argument of perigee of the satellite at epoch.
OMEGA0	Mean longitude of the ascending node of the satellite at epoch. Also known as right ascension of the ascending node.

Bstar	Drag coefficient of the satellite in units of (earth radii) ⁻¹ . Bstar is an adjusted value of the ballistic coefficient of the satellite, and it indicates how susceptible it is to atmospheric drag.
initialDateTime	Date-time string in UTC indicating the time corresponding to the known state vector of the satellite. It must be provided for objects in deep space, and also for objects near Earth if targetTime is provided as a date-time string.
targetTime	Time at which the position and velocity of the satellite should be calculated. It can be provided in two different ways: either as a number corresponding to the time in minutes counting from epoch at which the orbit should be propagated, or as a date-time string in UTC, in which case the date-time string for epoch must be provided through initialDateTime.
keplerAccuracy	Accuracy to consider Kepler's equation solved. If two consecutive solutions differ by a value lower than this accuracy, integration is considered to have converged.
maxKeplerIterations	Maximum number of iterations after which fixed-point integration of Kepler's equation will stop, even if convergence according to the accuracy criterion has not been reached.

Value

A list with three elements. The first two elements represent the position and velocity of the satellite at the target time, in the TEME (True Equator, Mean Equinox) frame of reference. Position values are in km, and velocity values are in km/s. Each of these two elements contains three values, corresponding to the X, Y and Z components of position and velocity in this order. The third element indicates the algorithm used to propagate the orbit (sgp4 or sdp4).

References

<https://celestrak.org/NORAD/documentation/spacetrk.pdf> <http://www.celestrak.org/publications/aiaa/2006-6753/AIAA-2006-6753.pdf>

Examples

```
# The following orbital parameters correspond to an object with NORAD catalogue
# number 24208 (Italsat 2) the 26th of June, 2006 at 00:58:29.34 UTC.

n0 <- 1.007781*((2*pi)/(1440)) # Multiplication by 2pi/1440 to convert to radians/min
e0 <- 0.002664 # mean eccentricity at epoch
i0 <- 3.8536*pi/180 # mean inclination at epoch in radians
M0 <- 48.3*pi/180 # mean anomaly at epoch in radians
omega0 <- 311.0977*pi/180 # mean argument of perigee at epoch in radians
OMEGA0 <- 80.0121*pi/180 # mean longitude of ascending node at epoch in radians
Bstar <- 1e-04 # drag coefficient
epochDateTime <- "2006-06-26 00:58:29.34"

# Calculation of the orbital period
```

```

2*pi/n0

# The period is higher than 225 min, and therefore the SDP4 model should be
# applied. Lets calculatethe position and velocity of the satellite 12 hours
# after epoch.

italsat_12h <- sgdp4(n0=n0, e0=e0, i0=i0, M0=M0, omega0=omega0, OMEGA0=OMEGA0,
                  Bstar=Bstar, initialDateTime=epochDateTime, targetTime=0)
italsat_12h$algorithm

# The SDP4 model was correctly chosen.

```

sgp4

Propagate an orbital state vector with the SGP4 model

Description

Given an orbital state vector of a satellite, applies the SGP4 model to propagate its orbit to the desired time point. This allows the calculation of the position and velocity of the satellite at different times, both before and after the time corresponding to the known state vector (referred to as "epoch"). Kepler's equation is solved through fixed-point integration. The SGP4 model can only accurately propagate the orbit of objects near Earth (with an orbital period shorter than 225 minutes, corresponding approximately to an altitude lower than 5877.5 km). For propagation of objects in deep space, the SDP4 model should be used, available through the [sdp4](#) function. This implementation is based on the theory and implementation described in Space Track Report #3, and includes the corrections summarized in Revisiting Space Track Report #3.

Usage

```
sgp4(n0, e0, i0, M0, omega0, OMEGA0, Bstar, initialDateTime=NULL, targetTime,
     keplerAccuracy=10e-12, maxKeplerIterations=10)
```

Arguments

n0	Mean motion of the satellite at epoch in radians/min.
e0	Mean eccentricity of the orbit of the satellite at epoch. Eccentricity ranges from 0 (perfectly circular orbit) to 1 (parabolic trajectory).
i0	Mean orbital inclination of the satellite at epoch in radians.
M0	Mean anomaly of the satellite at epoch.
omega0	Mean argument of perigee of the satellite at epoch.
OMEGA0	Mean longitude of the ascending node of the satellite at epoch. Also known as right ascension of the ascending node.
Bstar	Drag coefficient of the satellite in units of (earth radii) ⁻¹ . Bstar is an adjusted value of the ballistic coefficient of the satellite, and it indicates how susceptible it is to atmospheric drag.

<code>initialDateTime</code>	Optional date-time string in UTC indicating the time corresponding to the known state vector of the satellite. It must be provided if <code>targetTime</code> is provided as a date-time string.
<code>targetTime</code>	Time at which the position and velocity of the satellite should be calculated. It can be provided in two different ways: either as a number corresponding to the time in minutes counting from epoch at which the orbit should be propagated, or as a date-time string in UTC, in which case the date-time string for epoch must be provided through <code>initialDateTime</code> .
<code>keplerAccuracy</code>	Accuracy to consider Kepler's equation solved. If two consecutive solutions differ by a value lower than this accuracy, integration is considered to have converged.
<code>maxKeplerIterations</code>	Maximum number of iterations after which fixed-point integration of Kepler's equation will stop, even if convergence according to the accuracy criterion has not been reached.

Value

A list with three elements. The first two elements represent the position and velocity of the satellite at the target time, in the TEME (True Equator, Mean Equinox) frame of reference. Position values are in km, and velocity values are in km/s. Each of these two elements contains three values, corresponding to the X, Y and Z components of position and velocity in this order. The third element indicates the algorithm used to propagate the orbit (sgp4).

References

<https://celestrak.org/NORAD/documentation/spacetrk.pdf> <http://www.celestrak.org/publications/aiaa/2006-6753/AIAA-2006-6753.pdf>

Examples

```
# The following orbital parameters correspond to an object with NORAD catalogue
# number 88888 the 1st of October, 1980 at 23:41:24 UTC.

n0 <- 16.05824518*((2*pi)/(1440)) # Multiplication by 2pi/1440 to convert to radians/min
e0 <- 0.0086731 # mean eccentricity at epoch
i0 <- 72.8435*pi/180 # mean inclination at epoch in radians
M0 <- 110.5714*pi/180 # mean anomaly at epoch in radians
omega0 <- 52.6988*pi/180 # mean argument of perigee at epoch in radians
OMEGA0 <- 115.9689*pi/180 # mean longitude of ascending node at epoch in radians
Bstar <- 0.66816e-4 # drag coefficient

# Calculation of the orbital period

2*pi/n0

# The period is lower than 225 min, and therefore the SGP4 model is valid.
# Lets calculate the position and velocity of the satellite 40 minutes after
# epoch
```

```
new_state <- sgp4(n0=n0, e0=e0, i0=i0, M0=M0, omega0=omega0, OMEGA0=OMEGA0,
                 Bstar=Bstar, targetTime = 40)
new_state
```

 TEMetoGCRF

Convert coordinates from TEME to GCRF

Description

The TEME (True Equator, Mean Equinox) and GCRF (Geocentric Celestial Reference Frame) are both ECI frames of reference, i.e., Earth-centered inertial coordinate frames, where the origin is placed at the center of mass of Earth and the coordinate frame is fixed with respect to the stars (and therefore not fixed with respect to the Earth surface in its rotation).

The difference between the two resides in the fact that in the GCRF frame, the X-axis and Z-axis are aligned respectively with the mean equinox and rotation axis of Earth at 12:00 Terrestrial Time on the 1st of January, 2000, while in the TEME frame they are aligned with the mean equinox and rotation axis at the time of the corresponding TLE. Due to the change of the direction of the vernal equinox and the rotation axis over time, coordinates in the two frames differ slightly.

This function requires the `asterRiskData` package, which can be installed by running `install.packages('asterRiskData', repos='https://rafael-ayala.github.io/drat/')`

Usage

```
TEMetoGCRF(position_TEME, velocity_TEME, dateTime)
```

Arguments

<code>position_TEME</code>	Vector with the X, Y and Z components of the position of an object in TEME frame, in m.
<code>velocity_TEME</code>	Vector with the X, Y and Z components of the velocity of an object in TEME frame, in m/s.
<code>dateTime</code>	Date-time string with the date and time in UTC corresponding to the provided position and velocity vectors. This specifies the time for which the conversion from TEME to GCRF coordinates will be performed. It is required due to the change in the exact position of the rotation axis of Earth due to precession, nutation and polar motion.

Value

A list with two elements representing the position and velocity of the satellite in the ECEF (Earth Centered, Earth Fixed) frame of reference. Position values are in m, and velocity values are in m/s. Each of the two elements contains three values, corresponding to the X, Y and Z components of position and velocity in this order.

References

<https://celestrak.org/columns/v04n03/#FAQ01>

Examples

```
if(requireNamespace("asteRiskData", quietly = TRUE)) {
# The following orbital parameters correspond to an object with NORAD catalogue
# number 24208 (Italsat 2) the 26th of June, 2006 at 00:58:29.34 UTC.

n0 <- 1.007781*((2*pi)/(1440)) # Multiplication by 2pi/1440 to convert to radians/min
e0 <- 0.002664 # mean eccentricity at epoch
i0 <- 3.8536*pi/180 # mean inclination at epoch in radians
M0 <- 48.3*pi/180 # mean anomaly at epoch in radians
omega0 <- 311.0977*pi/180 # mean argument of perigee at epoch in radians
OMEGA0 <- 80.0121*pi/180 # mean longitude of ascending node at epoch in radians
Bstar <- 1e-04 # drag coefficient
epochDateTime <- "2006-06-26 00:58:29.34"

# Lets calculate the position and velocity of the satellite 1 day later

state_1day_TEME <- sgd4(n0=n0, e0=e0, i0=i0, M0=M0, omega0=omega0, OMEGA0=OMEGA0,
                      Bstar=Bstar, initialDateTime=epochDateTime, targetTime=1440)

# We can now convert the results in TEME frame to GCRF frame, previously
# multiplying by 1000 to convert the km output of sgd4 to m

state_1day_GCRF <- TEMEtoGCRF(state_1day_TEME$position*1000,
                              state_1day_TEME$velocity*1000,
                              "2006-06-27 00:58:29.34")
}
```

TEMEtoITRF

Convert coordinates from TEME to ITRF

Description

The TEME (True Equator, Mean Equinox) frame of reference is an Earth-centered inertial coordinate frame, where the origin is placed at the center of mass of Earth and the coordinate frame is fixed with respect to the stars (and therefore not fixed with respect to the Earth surface in its rotation). The coordinates and velocities calculated with the SGP4 and SDP4 models are in the TEME frame of reference. This function converts positions and velocities in TEME to the ITRF (International Terrestrial Reference Frame), which is an ECEF (Earth Centered, Earth Fixed) frame of reference. In the ITRF, the origin is also placed at the center of mass of Earth, but the frame rotates with respect to the stars to remain fixed with respect to the Earth surface as it rotates. The Z-axis extends along the true North as defined by the IERS reference pole, and the X-axis extends towards the intersection between the equator and the Greenwich meridian at any time.

This function requires the `asteRiskData` package, which can be installed by running `install.packages('asteRiskData', repos='https://rafael-ayala.github.io/drat/')`

Usage

```
TEMEtoITRF(position_TEME, velocity_TEME, dateTime)
```

Arguments

position_TEME	Vector with the X, Y and Z components of the position of an object in TEME frame, in m.
velocity_TEME	Vector with the X, Y and Z components of the velocity of an object in TEME frame, in m/s.
dateTime	Date-time string with the date and time in UTC corresponding to the provided position and velocity vectors. This specifies the time for which the conversion from TEME to ITRF coordinates will be performed. It is important to provide an accurate value, since the point over the surface of Earth to which a set of TEME coordinates refers varies with time due to the motion of Earth.

Value

A list with two elements representing the position and velocity of the satellite in the ITRF (International Terrestrial Reference Frame) frame of reference. Position values are in m, and velocity values are in m/s. Each of the two elements contains three values, corresponding to the X, Y and Z components of position and velocity in this order.

References

<https://celestrak.org/columns/v04n03/#FAQ01>

Examples

```
if(requireNamespace("asteRiskData", quietly = TRUE)) {
  # The following orbital parameters correspond to an object with NORAD catalogue
  # number 24208 (Italsat 2) the 26th of June, 2006 at 00:58:29.34 UTC.

  n0 <- 1.007781*((2*pi)/(1440)) # Multiplication by 2pi/1440 to convert to radians/min
  e0 <- 0.002664 # mean eccentricity at epoch
  i0 <- 3.8536*pi/180 # mean inclination at epoch in radians
  M0 <- 48.3*pi/180 # mean anomaly at epoch in radians
  omega0 <- 311.0977*pi/180 # mean argument of perigee at epoch in radians
  OMEGA0 <- 80.0121*pi/180 # mean longitude of ascending node at epoch in radians
  Bstar <- 1e-04 # drag coefficient
  epochDateTime <- "2006-06-26 00:58:29.34"

  # Lets calculate the position and velocity of the satellite 1 day later

  state_1day_TEME <- sgdp4(n0=n0, e0=e0, i0=i0, M0=M0, omega0=omega0, OMEGA0=OMEGA0,
                          Bstar=Bstar, initialDateTime=epochDateTime, targetTime=1440)

  # We can now convert the results in TEME frame to ITRF frame, previously
  # multiplying by 1000 to convert the km output of sgdp4 to m

  state_1day_ITRF <- TEMEtoITRF(state_1day_TEME$position*1000,
```

```

    state_1day_TEME$velocity*1000,
    "2006-06-27 00:58:29.34")
}

```

TEMEtoLATLON	<i>Convert coordinates from TEME to geodetic latitude, longitude and altitude</i>
--------------	---

Description

The TEME (True Equator, Mean Equinox) frame of reference is an Earth-centered inertial coordinate frame, where the origin is placed at the center of mass of Earth and the coordinate frame is fixed with respect to the stars (and therefore not fixed with respect to the Earth surface in its rotation). The coordinates and velocities calculated with the SGP4 and SDP4 models are in the TEME frame of reference. This function converts position in TEME to geodetic latitude, longitude and altitude, which can be considered to be a non-inertial, Earth-centered frame of reference.

Usage

```
TEMEtoLATLON(position_TEME, dateTime, degreesOutput=TRUE)
```

Arguments

position_TEME	Vector with the X, Y and Z components of the position of an object in TEME frame, in m.
dateTime	Date-time string with the date and time in UTC corresponding to the provided position vector. This specifies the time for which the conversion from TEME to geodetic coordinates will be performed. It is important to provide an accurate value, since the point over the surface of Earth to which a set of TEME coordinates refers varies with time due to the motion of Earth.
degreesOutput	Logical indicating if the output should be in sexagesimal degrees. If degreesOutput=FALSE, the output will be in radians.

Value

A vector with three elements, corresponding to the latitude and longitude in degrees (or radians if specified) and the altitude in m.

References

<https://arc.aiaa.org/doi/10.2514/6.2006-6753>

Index

calculateRazel, [3](#)

dateTimeToMJD, [4](#), [18](#)
deg2rad, [5](#)

ECItoKOE, [6](#)

GCRFtoITRF, [7](#)
GCRFtoLATLON, [9](#)
getLatestSpaceData, [10](#)

hpop, [8](#), [10](#), [11](#), [12](#)

ITRFtoGCRF, [15](#)
ITRFtoLATLON, [16](#)

JPLephemerides, [18](#)

KOEtoECI, [19](#)

LATLONtoGCRF, [21](#)
LATLONtoITRF, [22](#)

nanotime, [27](#), [32](#)

ode, [14](#)

parseTLElines, [23](#)

rad2deg, [25](#)
readGLONASSNavigationRINEX, [26](#)
readGPSNavigationRINEX, [28](#)
readOEM, [33](#)
readTLE, [35](#)
revDay2radMin, [37](#)

sdp4, [38](#), [40](#), [42](#)
sgdp4, [40](#)
sgp4, [38](#), [40](#), [42](#)

TEMEtoGCRF, [44](#)
TEMEtoITRF, [45](#)
TEMEtoLATLON, [47](#)