

# Package ‘FARS’

July 16, 2025

**Type** Package

**Title** Factor-Augmented Regression Scenarios

**Version** 0.5.0

**Maintainer** Gian Pietro Bellocca <gbellocc@est-econ.uc3m.es>

**Description** Provides a comprehensive framework in R for modeling and forecasting economic scenarios based on multi-level dynamic factor model. The package enables users to: (i) extract global and block-specific factors using a flexible multilevel factor structure; (ii) compute asymptotically valid confidence regions for the estimated factors, accounting for uncertainty in the factor loadings; (iii) estimate factor-augmented quantile regressions; (iv) recover full predictive densities from these quantile forecasts; and (v) estimate the density when the factors are stressed.

**Depends** R (>= 3.5.0)

**Imports** ggplot2, plotly, sn, nloptr, ellipse, SyScSelection, quantreg, tidyverse, dplyr,forcats, MASS, reshape2, stringr,

**Suggests** devtools, knitr, rmarkdown, markdown, openxlsx, readxl, zoo

**VignetteBuilder** knitr

**License** GPL (>= 2)

**Encoding** UTF-8

**RoxygenNote** 7.3.2

**URL** <https://arxiv.org/abs/2507.10679>

**NeedsCompilation** no

**Author** Gian Pietro Bellocca [aut, cre],  
Ignacio Garrón [aut],  
Vladimir Rodríguez-Caballero [aut],  
Esther Ruiz [aut]

**Repository** CRAN

**Date/Publication** 2025-07-16 08:50:06 UTC

## Contents

|                      |    |
|----------------------|----|
| compute_density      | 2  |
| compute_fars         | 3  |
| correct_outliers     | 5  |
| create_scenario      | 5  |
| mldfm                | 6  |
| mldfm_subsampling    | 8  |
| plot.fars            | 9  |
| plot.fars_density    | 10 |
| plot.mldfm           | 10 |
| print.fars           | 11 |
| print.fars_density   | 11 |
| print.mldfm          | 12 |
| quantile_risk        | 12 |
| summary.fars         | 13 |
| summary.fars_density | 13 |
| summary.mldfm        | 14 |

## Index

15

---

|                 |   |
|-----------------|---|
| compute_density | <i>Compute Skew-t Densities from Forecasted Quantiles</i> |
|-----------------|---|

---

### Description

Compute Skew-t Densities from Forecasted Quantiles

### Usage

```
compute_density(
  quantiles,
  levels = c(0.05, 0.25, 0.5, 0.75, 0.95),
  est_points = 512,
  random_samples = 5000,
  support = c(-10, 10),
  nl = FALSE,
  seed = NULL
)
```

### Arguments

- |            |   |
|------------|---|
| quantiles  | A matrix of forecasted quantiles. Each row is a time observation; each column a quantile level.   |
| levels     | A numeric vector of the quantile levels corresponding to the columns of the quantile matrix (default: c(0.05, 0.25, 0.50, 0.75, 0.95)). |
| est_points | Integer. Number of evaluation points for the estimated density (default: 512).  |

|                |  |
|----------------|--|
| random_samples | Integer. Number of random samples to draw from the fitted skew-t distribution (default: 5000).   |
| support        | Numeric vector of length 2. Defines the lower and upper limits of the density evaluation range. Used with est_points to create the evaluation grid. Default: c(-30, 10). |
| nl             | Logical. If TRUE, uses nonlinear optimization via nloptr; if FALSE, uses linear optimization via optim. Default: FALSE.  |
| seed           | Optional integer to set the random seed for reproducibility (default: NULL).   |

## Value

An object of class "fars\_density", which is a list containing the following components:

**density** A matrix of estimated densities for each time period (rows) across estimation points (columns).

**distribution** A matrix of random draws from the fitted skew-t distribution for each time period.

**optimization** The optimization method implemented.

**x\_vals** The sequence of evaluation points used to compute the density. Useful for plotting.

## Examples

```
Quantiles <- matrix(rnorm(500, mean = 0, sd = 1), nrow = 100, ncol = 5)
density_result <- compute_density(Quantiles, seed = 42)
```

compute\_fars

*Compute Factor Augmented Quantile Regressions and Stressed Quantiles*

## Description

Performs quantile regressions of a dependent variable on MLDFM-extracted factors. Optionally generates quantile forecasts under stressed scenarios using hyperellipsoids.

## Usage

```
compute_fars(
  dep_variable,
  factors,
  h = 1,
  edge = 0.05,
  scenario = NULL,
  min = TRUE,
  QTAU = 0.05
)
```

## Arguments

|                           |   |
|---------------------------|---|
| <code>dep_variable</code> | A numeric vector representing the dependent variable (e.g., GDP growth, inflation).   |
| <code>factors</code>      | A matrix of factor estimates from a <code>mldfm</code> model.   |
| <code>h</code>            | Integer. Forecast horizon (in time steps) for the quantile regression. Default is 1.  |
| <code>edge</code>         | Numeric. Trimming amount applied to the outermost quantiles (default <code>0.05</code> ).   |
| <code>scenario</code>     | Optional list of matrices representing a stressed scenario, as returned by <code>create_scenario()</code> .   |
| <code>min</code>          | Logical. If TRUE (default), implement a stepwise minimization. If FALSE, implement a stepwise maximization.   |
| <code>QTAU</code>         | Numeric. Quantile level (default <code>0.05</code> ) used to compute stressed factors via <code>compute_stressed_factors()</code> . Only used if <code>scenario</code> is provided. |

## Value

A list containing:

`Quantiles` Matrix of forecasted quantiles (rows = time, cols = quantile levels).

`Stressed_Quantiles` Matrix of stressed scenario quantiles (same format), returned only if `scenario` is provided.

`Coeff` Matrix of quantile regression coefficients for each quantile.

`Std. Error` Matrix of Std. Error for each regression coefficient.

`Pvalue` Matrix of p-values for each regression coefficient.

`QTAU` The quantile level used to compute stressed factors (if applicable).

`Stressed_Factors` Matrix of selected stressed factors (only if `scenario` is provided and `QTAU` is set).

## Examples

```
dep_variable <- rnorm(100) # A numeric vector
data <- matrix(rnorm(100*300), nrow = 100, ncol = 300)
block_ind <- c(150, 300) # Defines 2 blocks
global = 1
local <- c(1, 1)
mldfm_result <- mldfm(data, blocks = 2, block_ind = block_ind, global = global , local = local)
fars_result <- compute_fars(dep_variable, mldfm_result$Factors, h = 1, edge = 0.05)
```

---

|                  |                                      |
|------------------|--------------------------------------|
| correct_outliers | <i>Correct Outliers in a Dataset</i> |
|------------------|--------------------------------------|

---

## Description

This function identifies and corrects outliers in a dataset using principal component analysis (PCA). It scales the data, performs PCA, computes idiosyncratic components, and replaces values that fall outside a defined outlier threshold with the median of 5 previous values. The outlier threshold is determined using the interquartile range (IQR) method.

## Usage

```
correct_outliers(data, r)
```

## Arguments

|      |   |
|------|---|
| data | A numeric matrix or data frame where rows represent observations and columns represent variables. |
| r    | An integer specifying the number of principal components to use for PCA.                          |

## Value

A list containing:

|          |  |
|----------|--|
| data     | A matrix with corrected data where outliers are replaced by the median of previous values. |
| outliers | A binary matrix (same dimensions as the input data) indicating the position of outliers.   |

## Examples

```
data <- matrix(rnorm(100), nrow = 10, ncol = 10)
result <- correct_outliers(data, r = 3)
corrected_data <- result$data
outliers_matrix <- result$outliers
```

---

|                 |                                  |
|-----------------|----------------------------------|
| create_scenario | <i>Create Stressed Scenarios</i> |
|-----------------|----------------------------------|

---

## Description

Constructs confidence regions (hyperellipsoids) for the factor space based on a central MLDFM estimate and a set of subsampled estimates. These regions capture estimation uncertainty and are used to simulate stresses scenarios.

**Usage**

```
create_scenario(model, subsamples, alpha = 0.95, fpr = FALSE)
```

**Arguments**

|                         |  |
|-------------------------|--|
| <code>model</code>      | An object of class <code>mldfm</code> , containing the factor estimates.   |
| <code>subsamples</code> | A list of <code>mldfm</code> objects returned from <code>mldfm_subsampling</code> .  |
| <code>alpha</code>      | Numeric. Confidence level (level of stress) for the hyperellipsoid (e.g., 0.95).   |
| <code>fpr</code>        | Logical. If TRUE, uses the Adaptive Threshold Cross-Sectional Robust (FPR) Gamma as in Fresoli, Poncela and Ruiz (2024); otherwise, uses the standard time-varying (NG) Gamma. |

**Value**

A list of matrices representing the hyperellipsoid points for each time observation.

**Examples**

```
data <- matrix(rnorm(100*300), nrow = 100, ncol = 300)
block_ind <- c(150, 300) # Defines 2 blocks
global = 1
local <- c(1, 1)
mldfm_result <- mldfm(data, blocks = 2, block_ind = block_ind,
global = global, local = local)
mldfm_subsampling_result <- mldfm_subsampling(data, blocks = 2,
block_ind = block_ind, global = global,
local = local, n_samples = 100, sample_size = 0.9)
scenario <- create_scenario(mldfm_result, mldfm_subsampling_result,
alpha = 0.95)
```

**Description**

Estimates a multilevel dynamic factor model from time series data. Supports both single-block and hierarchical multi-block structures with customizable factor extraction settings.

**Usage**

```
mldfm(
  data,
  blocks = 1,
  block_ind = NULL,
  global = 1,
```

```

local = NULL,
middle_layer = NULL,
method = 0,
tol = 1e-06,
max_iter = 1000,
verbose = TRUE
)

```

## Arguments

|                           |  |
|---------------------------|--|
| <code>data</code>         | A numeric matrix or data frame containing the time series data. Rows represent time points; columns represent observed variables.          |
| <code>blocks</code>       | Integer. Number of blocks into which the data is divided.  |
| <code>block_ind</code>    | Integer vector. End column indices for each block. Must be of length <code>blocks</code> and in increasing order.                          |
| <code>global</code>       | Integer. Number of global factors extracted from the entire dataset.   |
| <code>local</code>        | Integer vector of length <code>blocks</code> . Specifies the number of local factors for each block.                                       |
| <code>middle_layer</code> | Named list. Each name is a string specifying a group of blocks (e.g., "1-3" or "2-3"), and each value is the number of factors to extract. |
| <code>method</code>       | Integer. Method used to initialize the factors: 0 for Canonical Correlation Analysis (CCA), 1 for Principal Component Analysis (PCA).      |
| <code>tol</code>          | Numeric. The tolerance level for the residual sum of squares (RSS) minimization process. Used as a convergence criterion.                  |
| <code>max_iter</code>     | Integer. The maximum number of iterations allowed for the RSS minimization process.  |
| <code>verbose</code>      | Logical. If TRUE (default), print a summary of the mldfm.  |

## Value

An object of class `mldfm`, which is a list containing the following components:

**Factors** Matrix of estimated factors.

**Lambda** Matrix of factor loadings.

**Residuals** Matrix of residuals.

**Iterations** Number of iterations before convergence.

**Factors\_list** List of estimated factors for each node.

## Examples

```

data <- matrix(rnorm(1000), nrow = 100, ncol = 519)
block_ind <- c(63, 311, 519) # Defines 3 blocks
local <- c(1, 1, 1)          # One local factor per block
middle_layer <- list("1-3" = 1)
result <- mldfm(data, blocks = 3, block_ind = block_ind, global = 1,
local = local, middle_layer = middle_layer)

```

```
summary(result)
```

**mldfm\_subsampling***Subsampling Procedure for MLDFM Estimation***Description**

Repeatedly applies the MLDFM estimation to randomly drawn subsamples of the input data.

**Usage**

```
mldfm_subsampling(
  data,
  blocks = 1,
  block_ind = NULL,
  global = 1,
  local = NULL,
  middle_layer = NULL,
  method = 0,
  tol = 1e-06,
  max_iter = 1000,
  n_samples = 10,
  sample_size = 0.9,
  seed = NULL
)
```

**Arguments**

|                     |  |
|---------------------|--|
| <b>data</b>         | A numeric matrix or data frame containing the time series data. Rows represent time points; columns represent observed variables.                    |
| <b>blocks</b>       | Integer. The number of blocks into which the data is divided.  |
| <b>block_ind</b>    | A vector of integers indicating the end index of each block. Must be of length <b>blocks</b> and in increasing order. Required if <b>blocks</b> > 1. |
| <b>global</b>       | Integer. Number of global factors extracted from the entire dataset.   |
| <b>local</b>        | Integer vector of length <b>blocks</b> . Specifies the number of local factors for each block.   |
| <b>middle_layer</b> | Named list. Each name is a string specifying a group of blocks (e.g., "1-3" or "2-3"), and each value is the number of factors to extract.           |
| <b>method</b>       | Integer. The method used to initialize the factors: 0 for Canonical Correlation Analysis (CCA), 1 for Principal Component Analysis (PCA).            |
| <b>tol</b>          | Numeric. The tolerance level for the residual sum of squares (RSS) minimization process. Used as a convergence criterion.                            |

|             |  |
|-------------|--|
| max_iter    | Integer. The maximum number of iterations allowed for the RSS minimization process.                                |
| n_samples   | Number of subsamples to generate.  |
| sample_size | Proportion of the original sample to retain (e.g., 0.9 for 90%).   |
| seed        | Optional integer. Seed for reproducibility of the subsampling process. If NULL, random draws will differ each run. |

**Value**

A list of `mldfm` objects, one for each subsample.

**Examples**

```
data <- matrix(rnorm(1000), nrow = 100, ncol = 100)
block_ind <- c(50,100) # Defines 3 blocks
local <- c(1, 1)
result <- mldfm_subsampling(data, blocks = 2, block_ind = block_ind, global = 1,
local = local, n_samples = 100, sample_size = 0.9)
```

**plot.fars***Plot Method for fars Object***Description**

Generates line plots of forecasted quantiles from a FARS object. If a stressed scenario is available, it is plotted in a separate panel.

**Usage**

```
## S3 method for class 'fars'
plot(x, dates = NULL, ...)
```

**Arguments**

|       |  |
|-------|--|
| x     | An object of class <code>fars</code> .   |
| dates | Optional vector of dates (as Date or zoo::yearqtr) to use for the x-axis. If not provided, a simple index is used. |
| ...   | Additional arguments (currently ignored).  |

**Value**

No return value. Called for plot generation.

**plot.fars\_density**      *Plot method for fars\_density objects*

### Description

Plots the evolution of the estimated density over time as a 3D surface.

### Usage

```
## S3 method for class 'fars_density'
plot(x, time_index = NULL, ...)
```

### Arguments

- |                         |   |
|-------------------------|---|
| <code>x</code>          | An object of class <code>fars_density</code> .              |
| <code>time_index</code> | Optional vector for the time axis (default is 1:nrow).      |
| <code>...</code>        | Additional arguments passed to the plot function. (ignored) |

### Value

An interactive plot of class `plotly`.

**plot.mldfm**      *Plot method for MLDFM object*

### Description

Dispatches to specific plot functions for factors, loadings, or residuals.

### Usage

```
## S3 method for class 'mldfm'
plot(x, which = "factors", dates = NULL, var_names = NULL, ...)
```

### Arguments

- |                        |  |
|------------------------|--|
| <code>x</code>         | An object of class <code>mldfm</code> .  |
| <code>which</code>     | What to plot: one of "factors" (default), "loadings", or "residuals".  |
| <code>dates</code>     | Optional vector of dates (as Date or zoo::yearqtr) to use for the x-axis. If not provided, a simple index (1:N) is used. |
| <code>var_names</code> | Optional vector of variable names to label loadings and residual axis.   |
| <code>...</code>       | Additional arguments (ignored)   |

### Value

No return value. Called for plots generation.

---

print.fars                    *Print method for fars object*

---

**Description**

Prints a short summary of the fars object

**Usage**

```
## S3 method for class 'fars'  
print(x, ...)
```

**Arguments**

|     |                                    |
|-----|------------------------------------|
| x   | An object of class fars_quantiles. |
| ... | Additional arguments (ignored).    |

**Value**

The input object x, returned invisibly.

---

print.fars\_density        *Print method for fars\_density objects*

---

**Description**

Displays a brief summary of the density estimation object produced by the density() or nl\_density() function.

**Usage**

```
## S3 method for class 'fars_density'  
print(x, ...)
```

**Arguments**

|     |                                  |
|-----|----------------------------------|
| x   | An object of class fars_density. |
| ... | Additional arguments (ignored).  |

**Value**

The input object x, returned invisibly.

`print.mldfm` *Print Method for MLDFM Object*

### Description

Prints a short summary of the multilevel dynamic factor model

### Usage

```
## S3 method for class 'mldfm'
print(x, ...)
```

### Arguments

|                  |   |
|------------------|---|
| <code>x</code>   | An object of class <code>mldfm</code> . |
| <code>...</code> | Additional arguments (ignored).         |

### Value

The input object `x`, invisibly.

`quantile_risk` *Extract Conditional Quantile from Simulated Densities*

### Description

Computes the conditional quantile (e.g., 5th percentile) from a simulated skew-t distribution, generated via `density()` or `nl_density()`. The result corresponds to the risk measure (e.g., Growth-at-Risk, Growth-in-Stress etc.).

### Usage

```
quantile_risk(density, QTAU = 0.05)
```

### Arguments

|                      |  |
|----------------------|--|
| <code>density</code> | An object of class <code>fars_density</code> returned by <code>density()</code> or <code>nl_density()</code> . |
| <code>QTAU</code>    | A numeric value between 0 and 1 indicating the quantile to extract (e.g., 0.05 for 5th percentile).            |

### Value

A numeric vector of conditional quantiles (one observation for each time period).

**Examples**

```
Quantiles <- matrix(rnorm(500), ncol = 5)
fars_density <- compute_density(Quantiles, seed = 42)
GaR <- quantile_risk(fars_density, QTAU = 0.05)
```

---

**summary.fars***Summary Method for fars Object*

---

**Description**

Prints a complete summary of the fars object.

**Usage**

```
## S3 method for class 'fars'
summary(object, ...)
```

**Arguments**

- |        |                                    |
|--------|------------------------------------|
| object | An object of class fars_quantiles. |
| ...    | Additional arguments (ignored).    |

**Value**

The input object object, returned invisibly.

---

**summary.fars\_density** *Summary method for fars\_density objects*

---

**Description**

Provides summary statistics of the density estimation for each time observation, including the mean, median, and standard deviation of the simulated distribution.

**Usage**

```
## S3 method for class 'fars_density'
summary(object, ...)
```

**Arguments**

- |        |                                  |
|--------|----------------------------------|
| object | An object of class fars_density. |
| ...    | Additional arguments (ignored).  |

**Value**

A data frame with one row per time observation and columns: Observation, Mean, Median, and StdDev. The object is also printed to the console and returned invisibly.

---

summary.mldfm                   *Summary Method for MLDFM Object*

---

**Description**

Provides a complete summary of the multilevel dynamic factor model

**Usage**

```
## S3 method for class 'mldfm'  
summary(object, ...)
```

**Arguments**

|        |   |
|--------|---|
| object | An object of class <code>mldfm</code> . |
| ...    | Additional arguments (ignored).         |

**Value**

The input object `object`, invisibly.

# Index

compute\_density, 2  
compute\_fars, 3  
correct\_outliers, 5  
create\_scenario, 5  
  
mldfm, 6  
mldfm\_subsampling, 8  
  
plot.fars, 9  
plot.fars\_density, 10  
plot.mldfm, 10  
print.fars, 11  
print.fars\_density, 11  
print.mldfm, 12  
  
quantile\_risk, 12  
  
summary.fars, 13  
summary.fars\_density, 13  
summary.mldfm, 14